Course Syllabus Fourier Analysis and Fractals BMETE957306

Instructor Information:

Instructor: Prof. Károly Simon, www.math.bme.hu/~simonk, simonk@math.bme.hu Time and Place: The course held fully online on Microsoft teams. All information about the course: http://www.math.bme.hu/~simonk/ff Language of instruction: English Attendance and Class Participation: No attendance requirements for Covid-19, Text in English: (1) K. Falconer, Fractal Geometry, Wiley, 2003 (2) K. Falconer, The geometry of fractal sets, Cambridge, 1985

- (3) K Falconer, Techniques in fractal geometry, Wiley, 1997,
- (4) Pertti Mattila, Fourier Analysis and Hausdorff Dimension, Cambridge 2015.
- (5) Pertti Mattila, Geometry of Sets and Measures in Euclidean Spaces, Cambridge 1995.
- (6) T. Wolf, Lectures in Harmonic analysis, AMS, revised 2002.

Slides of the lectures of the course might be be available at:

http://www.math.bme.hu/~simonk/ff

Prerequisites: No prerequisites for MSc and PhD students. Measure Theory for BSc students.

Final exam: The final exam will consists of the theorems, definitions proofs and exercises, which are very similar to the ones we discussed in class.

Grading policy:

Final exam: 100 %. Grading Scale:

| Fail (1) | 0 -39 | % |
|------------------|--------|---|
| Pass(2) | 40-54 | % |
| Satisfactory (3) | 55-69 | % |
| Good (4) | 70-84 | % |
| Excellent (5) | 85-100 | % |

Topics:

- (1) The best-known examples of self-similar and self-affine fractals.
- (2) Hausdorff and Box-dimension. (Definition and properties.)
- (3) A brief review of measure theory and covering theorems.
- (4) Energy, Capacity and Frostman Lemma.
- (5) The dimension of the orthogonal projections of sets and measures, the transversality method.
- (6) The connection between the fact that a measure is absolute continuous with L^2 density and the fact that its Fourier transform is in L^2 .
- (7) Bernoulli convolutions.
- (8) Salem sets and Fourier dimension.
- (9) Falconer's distance set conjectures.
- (10) Peres-Schlag generalized transversality method.
- (11) Hochman Theorem about the dimension of self-similar measures on the line.
- (12) Shmerkin-Solomyak Theorem about the absolute continuity of self-similar measures.
- (13) The dimension of the trajectory of Brownian motion.

Prof. Károly Simon, 30 August, 2020.