## Calculus 1 - Homework 4

1. (9 points) Let $f(x)=(x-2)^{3}(x+3)^{2}$
a) Determine the intervals where the function increases or decreases.
b) Find the local extreme values of the function.
c) Find the global extreme values of $f$ on the interval $[-4,1]$.
2. (8 points) Find the inflection points of the function $f(x)=\left(x^{2}-2\right) e^{-x}$.
a) Determine the intervals where the function is convex or concave.
b) Find the inflection points of the function.
3. (8 points) You want to make a cylindrical tin cup with closed top of volume 1 liter. What is the minimal possible surface area of the cup?
4.* (8 points) The widths of two perpendicular corridors are 2.4 m and 1.6 m , respectively. What is the longest ladder that can be moved (in a horizontal position) from one corridor to another?

Deadline: December 12th.

