

DATA-BASED MODELING:

System Identification in practice

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- Introduction
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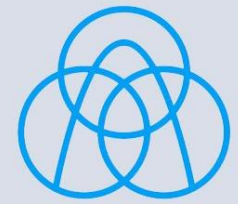
- System identification cycle
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- Applications in the automotive industry
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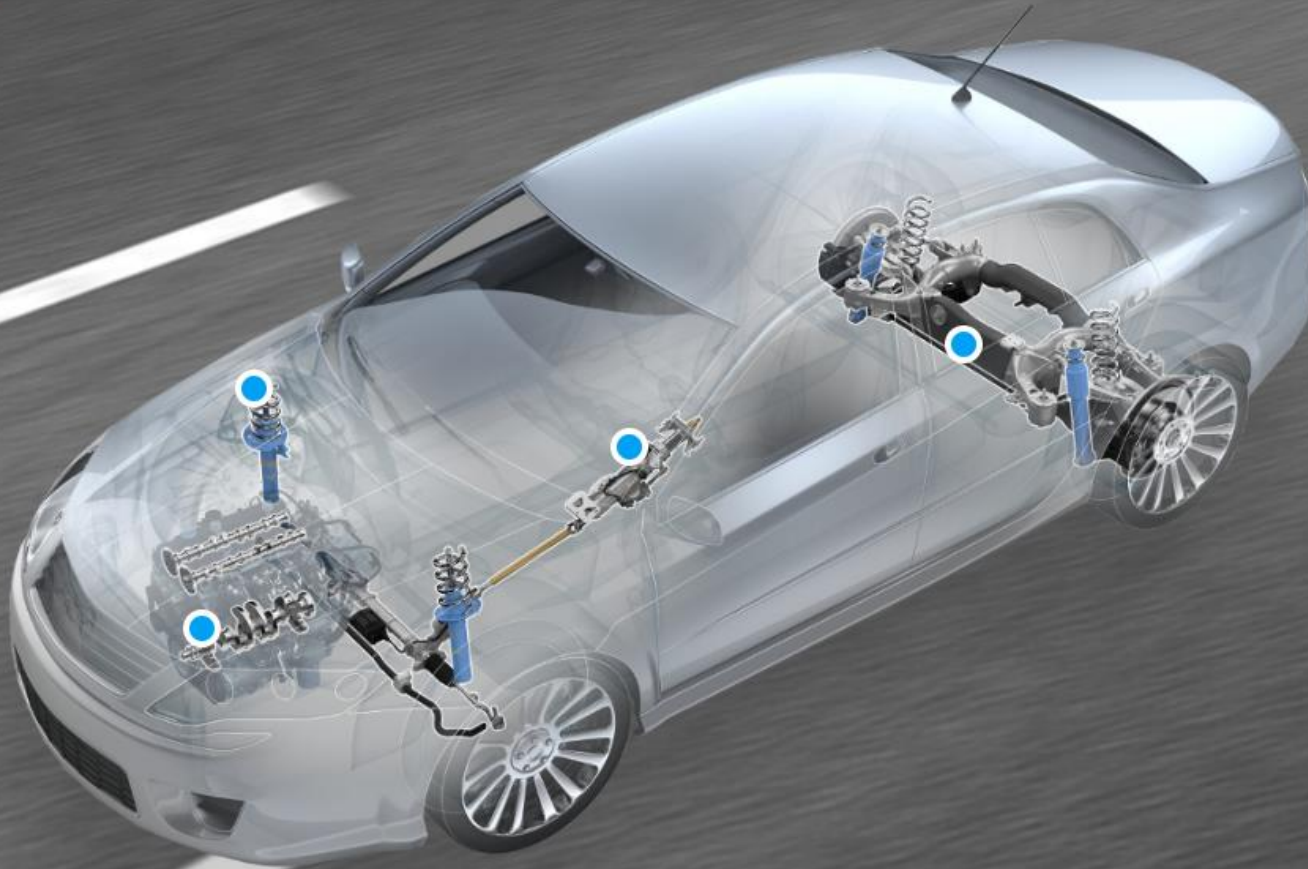
- Example

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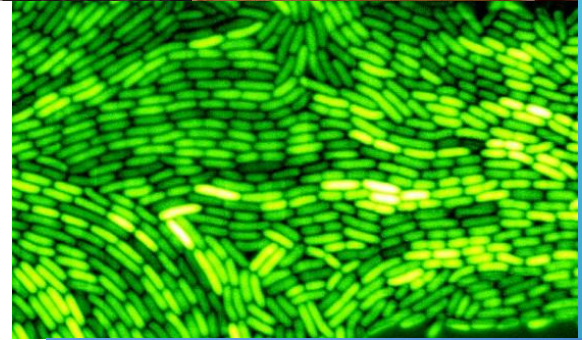


thyssenkrupp



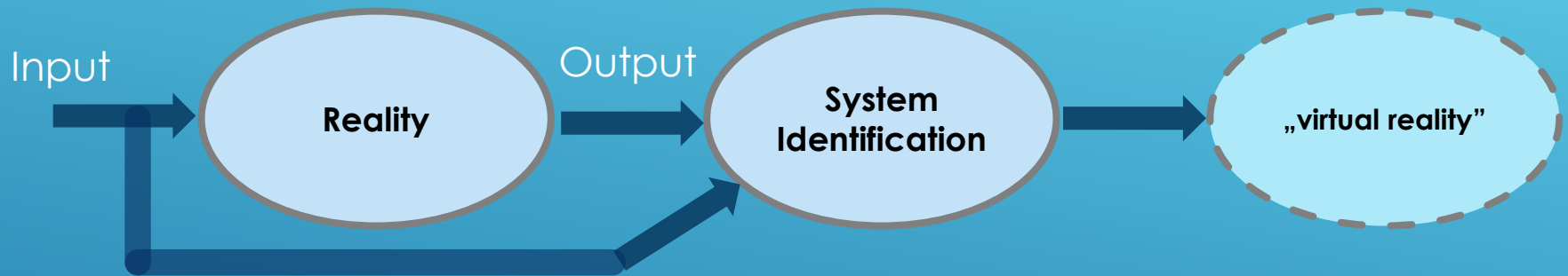
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INTRODUCTION



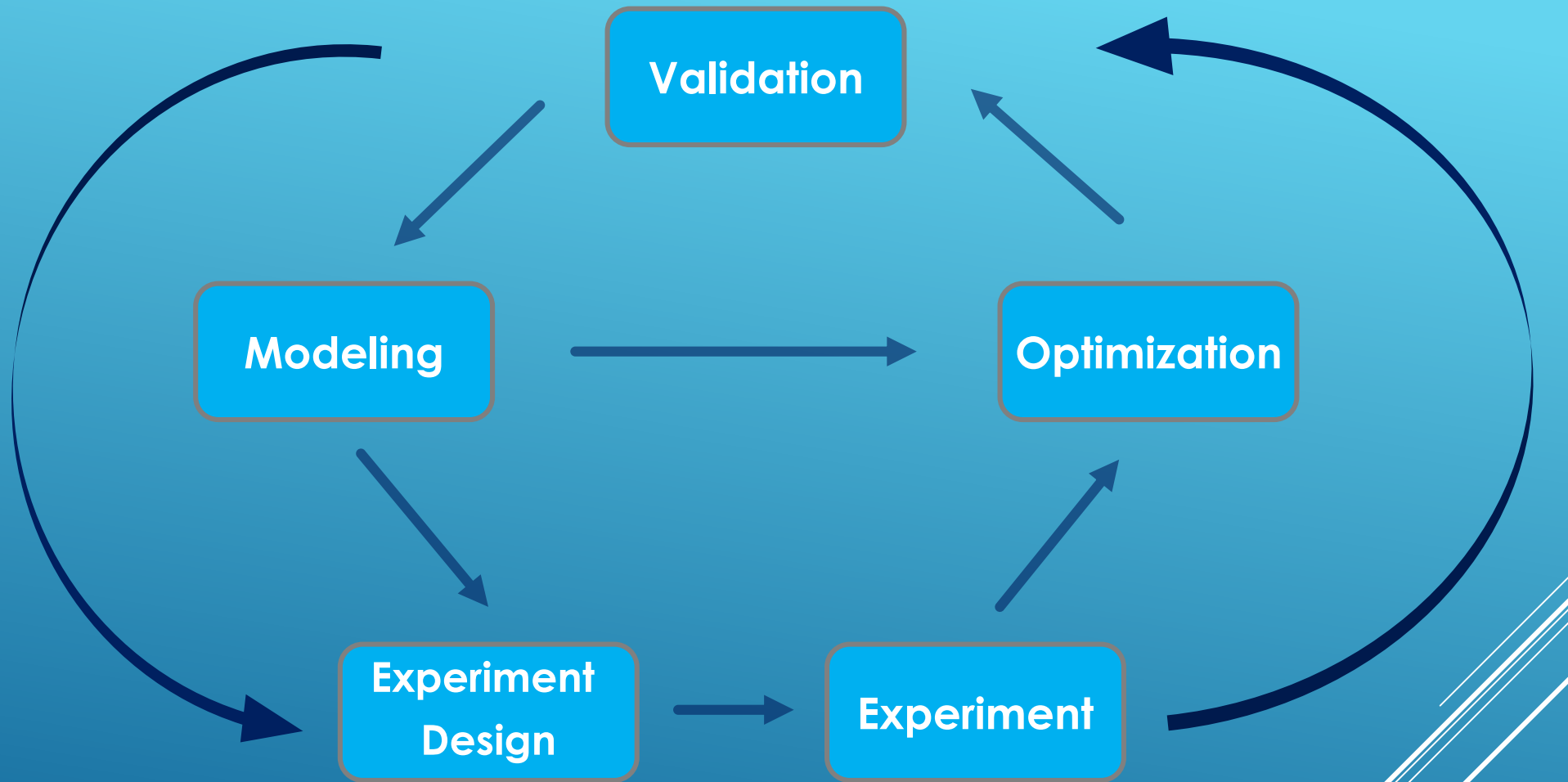
SYSTEM IDENTIFICATION

- ▶ Basically, how to represent the reality in the virtual space as mathematical model based on measurements:

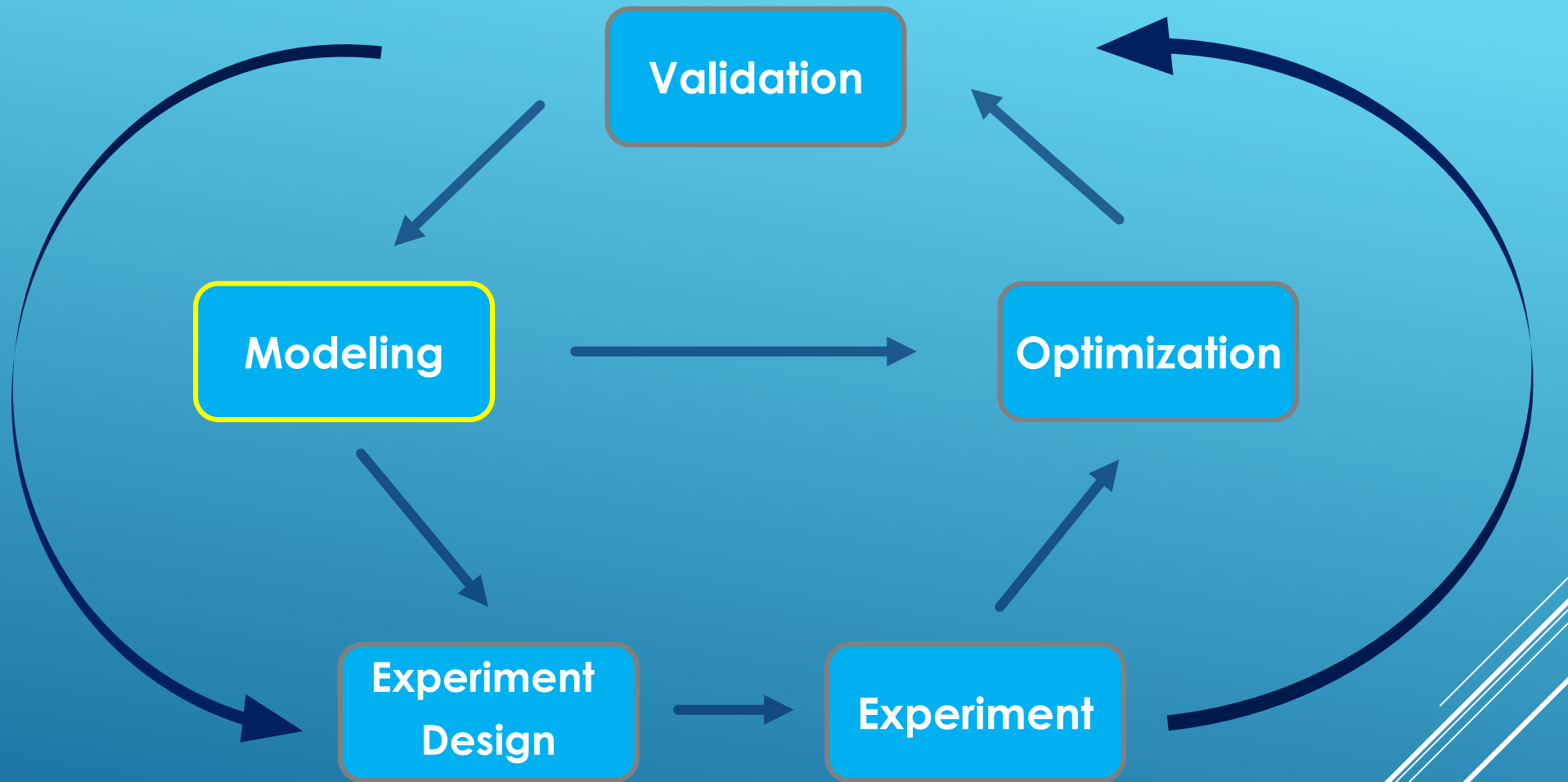


- ▶ Which can be used to predict/simulate the behavior of the reality in a much compact and cheaper way.

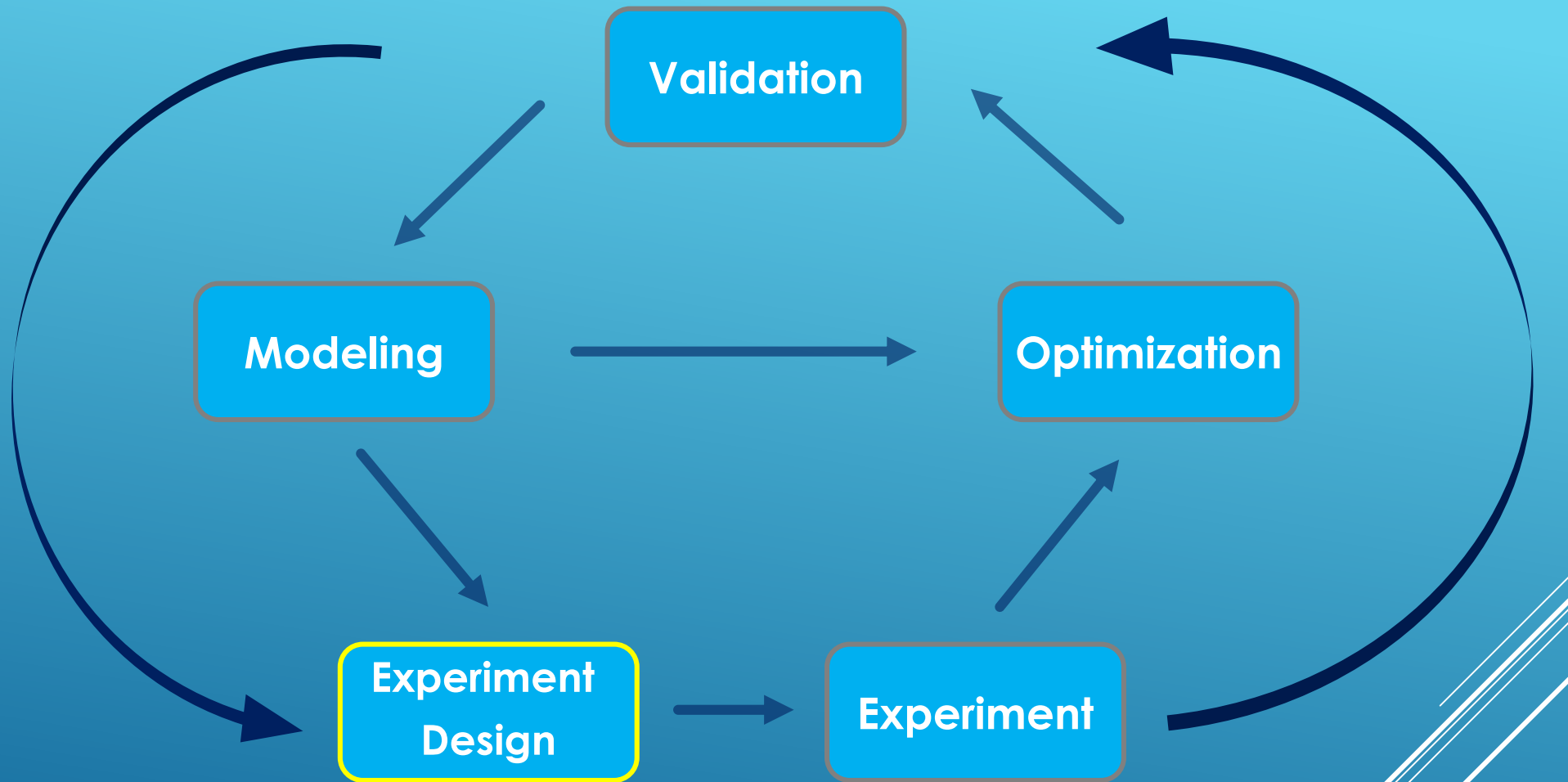
SYSTEM IDENTIFICATION



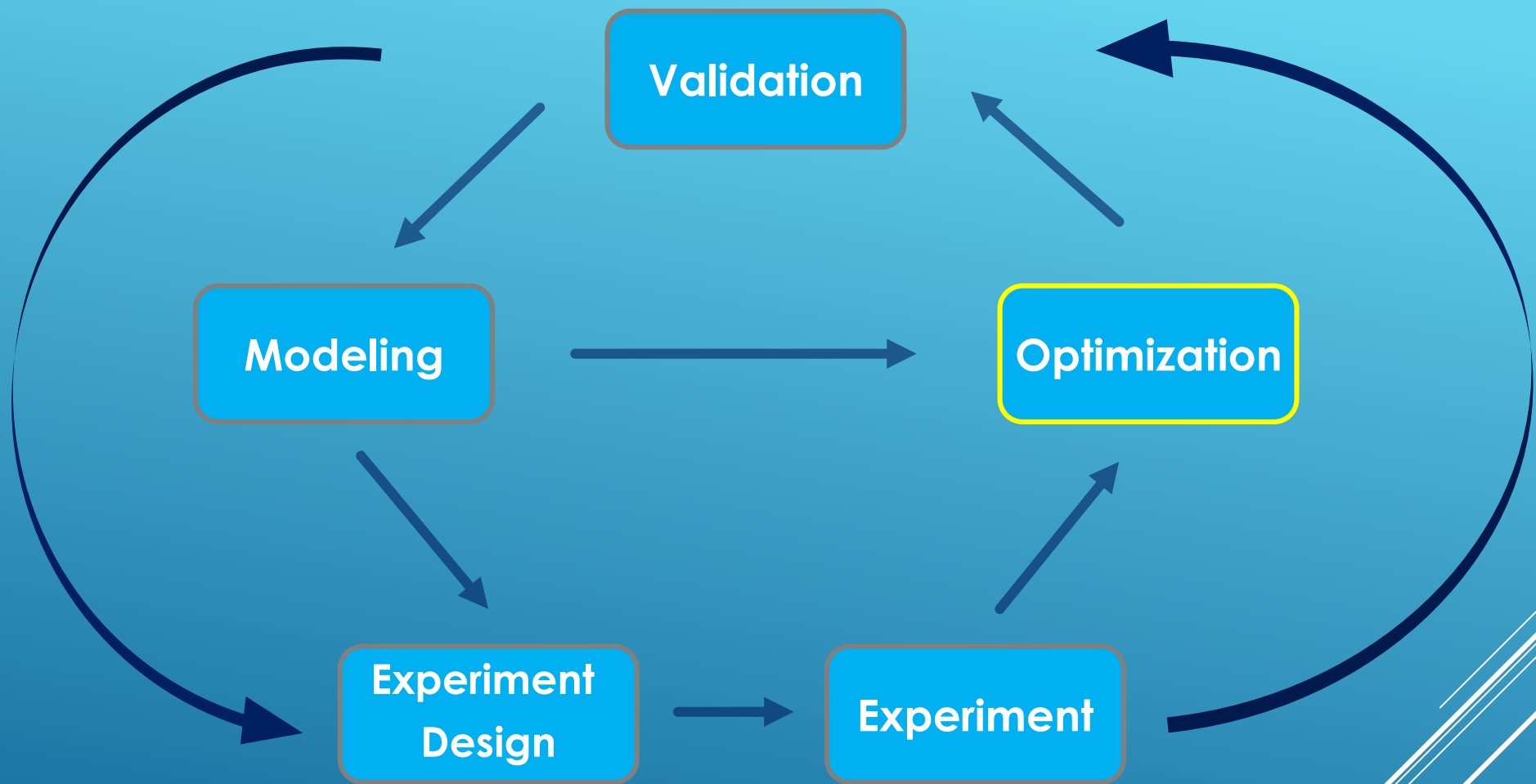
SYSTEM IDENTIFICATION



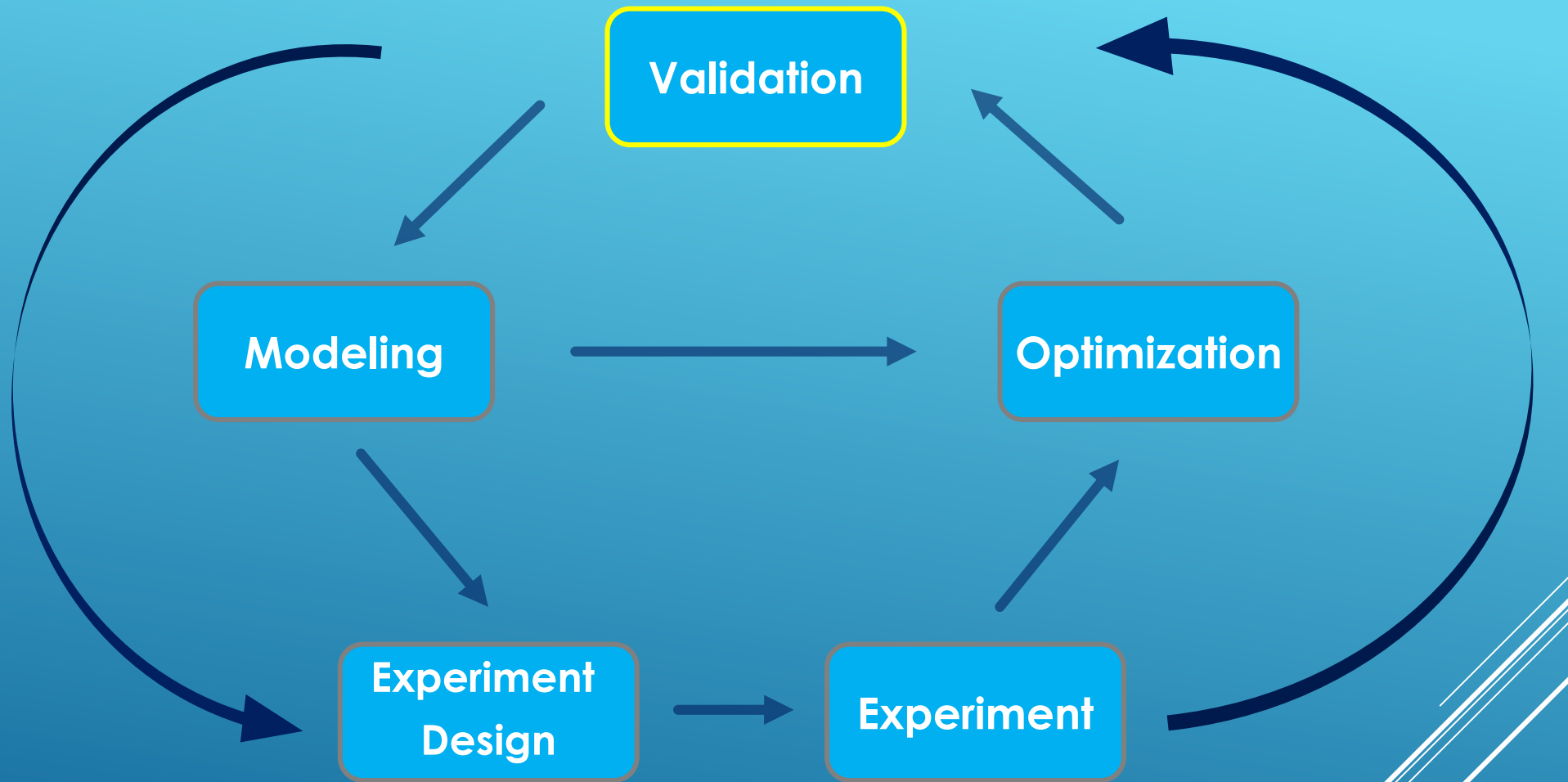
SYSTEM IDENTIFICATION



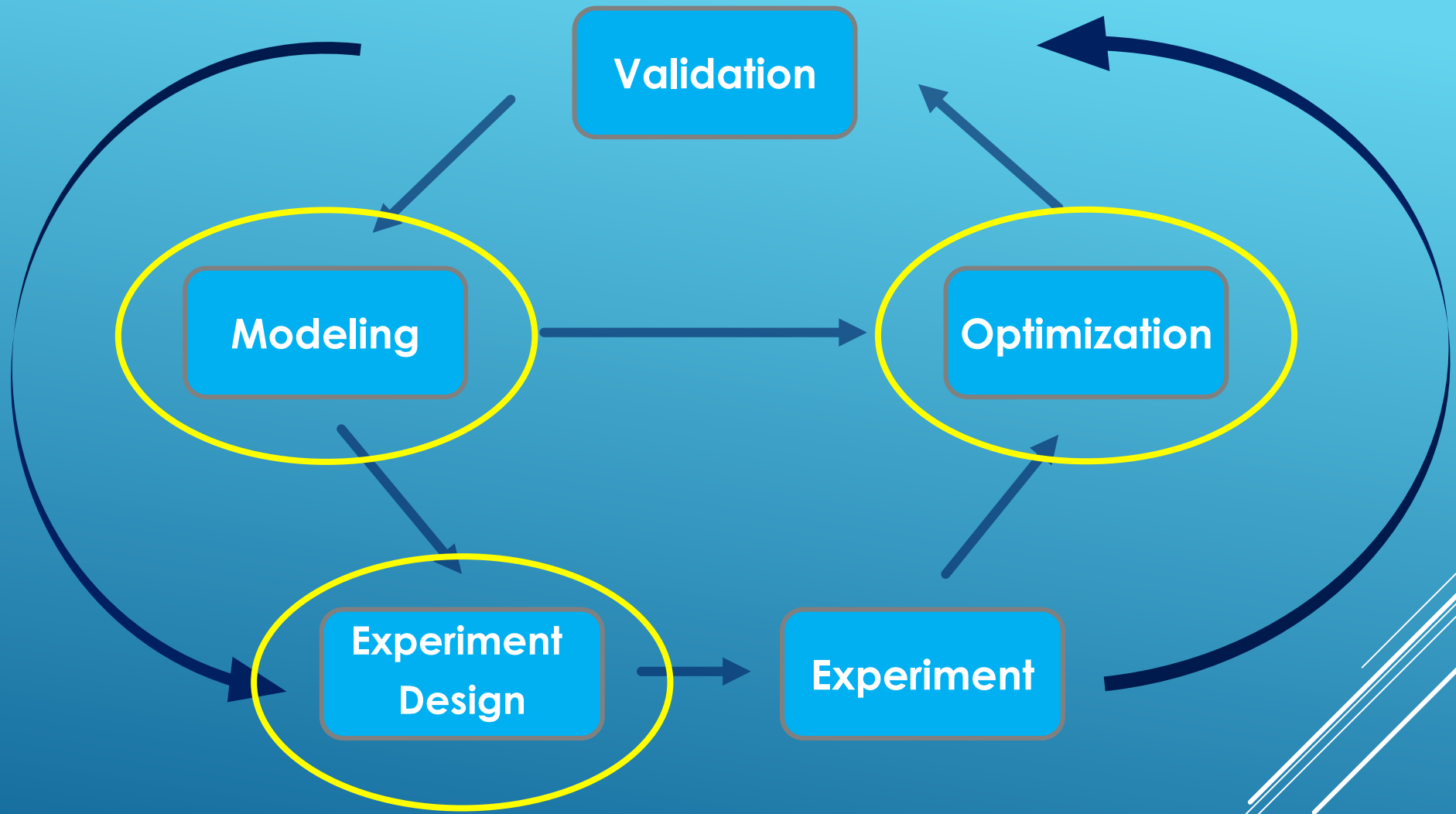
SYSTEM IDENTIFICATION



SYSTEM IDENTIFICATION



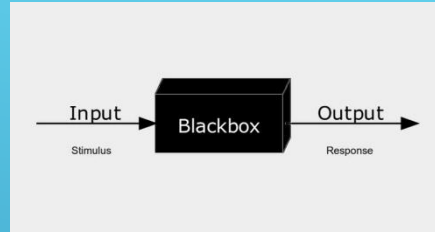
SYSTEM IDENTIFICATION



SYSTEM IDENTIFICATION

▶ Black-box

- ▶ Input/output behavior



▶ White-box

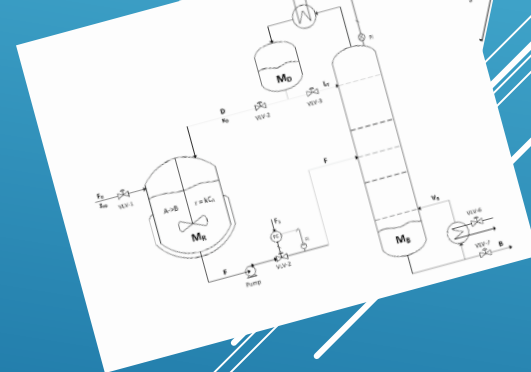
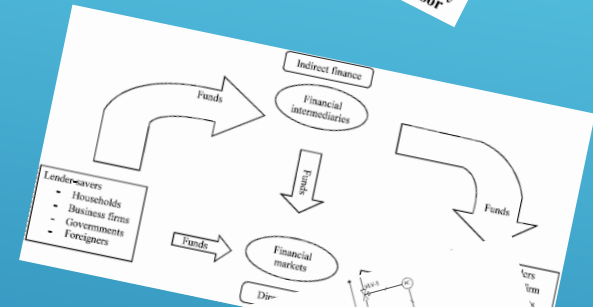
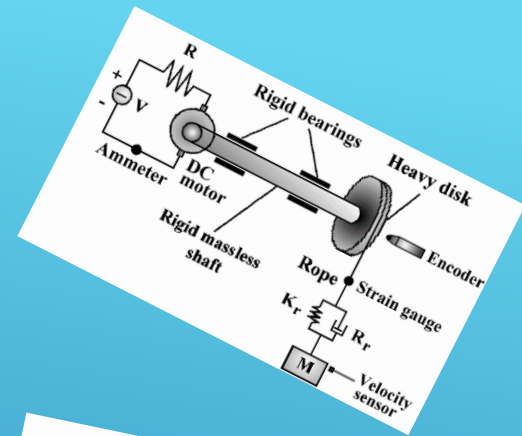
- ▶ Model is created based on the field specific knowledge: differential equations, reaction equations, etc...

▶ Frequency-domain representation

- ▶ Integral transformed linear differential equation.
- ▶ Discrete-time models are applied usually for computational purposes.

▶ Identifiability

- ▶ Which makes modeling the most crucial step in identification.



MODELING

- ▶ How to excite the system in order to get the most information possible?
 - ▶ Can contain also optimization.
 - ▶ Select the best input signal (magnitude, shape and frequency)

- ▶ Perform the activity that is needed to gather the data for identification and validation.
 - ▶ Highly process dependent task.
 - ▶ Physical measurements.
 - ▶ Big-data analysis.
 - ▶ ...

EXPERIMENT

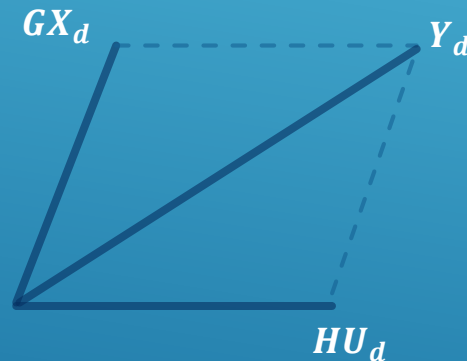
- ▶ The frontline application of numerical mathematics
 - ▶ Classical parameter estimation using least squares for dynamic systems in time- and frequency domain.

$$J(\boldsymbol{\theta}) = \frac{1}{N} \sum_{k=0}^{N-1} \|\mathbf{y}(k) - \hat{\mathbf{y}}(k, \boldsymbol{\theta})\|^2$$

- ▶ $\hat{\mathbf{y}}(k, \boldsymbol{\theta})$ can be generated using a large set of different models.
 - ▶ Modern one-step method using subspace-based techniques.

$$\begin{aligned} \mathbf{x}_{k+1} &= \mathbf{A}\mathbf{x}_k + \mathbf{B}\mathbf{u}_k \\ \mathbf{y}_k &= \mathbf{C}\mathbf{x}_k + \mathbf{D}\mathbf{u}_k \end{aligned}$$

$$\mathbf{Y}_d = \mathbf{G}\mathbf{X}_d + \mathbf{H}\mathbf{U}_d$$



- ▶ Recursive subspace-based techniques.

- ▶ Check if the model behaves similarly (within an error range of acceptance) as the reality does.
 - ▶ This step contains simulation of the estimated model based on experimental data gathered on the real system.

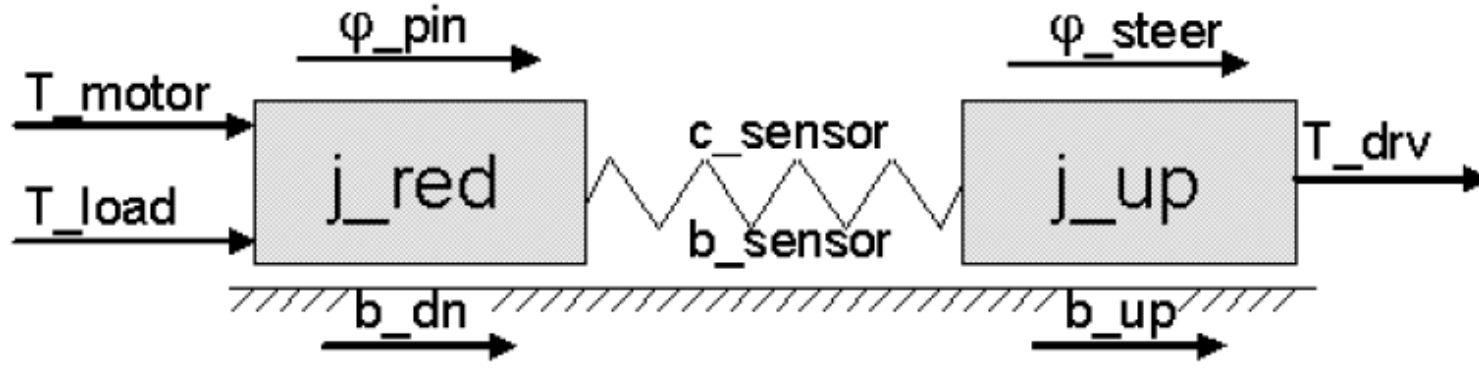
VALIDATION



- ▶ Permanent magnet synchronous motor parameter identification for motor control purposes:

$$\mathbf{f} \left(\begin{bmatrix} i_d \\ i_q \\ \omega \end{bmatrix} \right) = \begin{bmatrix} \frac{-Ri_d + n_p \omega L_q i_q}{L_d} \\ \frac{-Ri_q - n_p \omega L_d i_d - n_p \omega K_g}{L_q} \\ \frac{3n_p}{2j_{mot}} (i_q K_g + i_q i_d (L_d - L_q)) - \frac{b_{mot}}{j_{mot}} \omega \end{bmatrix}$$

$$\mathbf{g} \left(\begin{bmatrix} i_d \\ i_q \\ \omega \end{bmatrix} \right) = \begin{bmatrix} \frac{1}{L_d} & 0 & 0 \\ 0 & \frac{1}{L_q} & 0 \\ 0 & 0 & -\frac{1}{j_{mot}} \end{bmatrix}$$



$$\dot{x} = A(\theta)x + B(\theta)u$$

$$y = C(\theta)x + D(\theta)u$$

APPLICATION IN TKP

Dynamic equations:

$$j_{up}\dot{\omega}_{stw}(t) = T_{drv}(t) - T_{stc}(t) - T_{damp,up}(t)$$

$$j_{dn}\dot{\omega}_{pin}(t) = T_{stc}(t) + i_{gear}T_{mot}(t) + T_{load}(t) - T_{damp,dn}(t)$$

$$\dot{T}_{mot}(t) = \frac{1}{\tau} (T_{mot,req}(t) - T_{mot}(t))$$

Algebraic equations:

$$T_{stc}(t) = c_{sensor} (\varphi_{stw}(t) - \varphi_{pin}(t)) + b_{sensor} (\omega_{stw}(t) - \omega_{pin}(t))$$

$$T_{damp,up}(t) = b_{up}\omega_{stw}(t)$$

$$T_{damp,dn}(t) = b_{dn}\omega_{pin}(t)$$

$$T_{TSU} = c_{sensor} (\varphi_{stw}(t) - \varphi_{pin}(t))$$

$$\omega_{mot} = i_{gear}\omega_{pin}$$

APPLICATION IN TKP

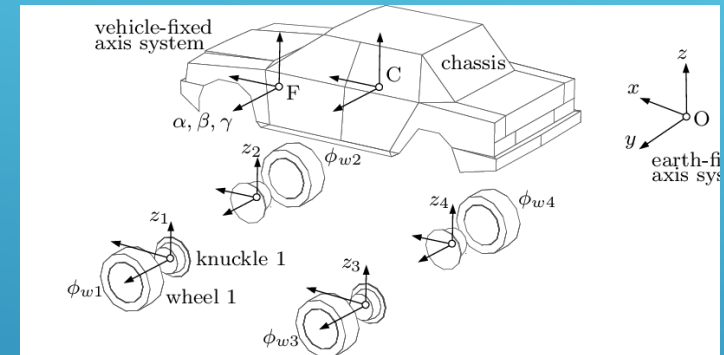
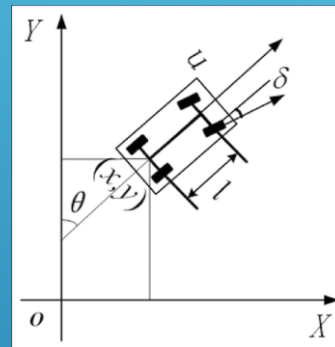
$$\begin{bmatrix} \dot{\varphi}_{pin} \\ \dot{\omega}_{pin} \\ \Delta\varphi \\ \ddot{\Delta\varphi} \\ \dot{T}_{mot} \end{bmatrix} = \begin{bmatrix} 0 & 1 & 0 & 0 & 0 \\ 0 & -\frac{b_{dn}}{j_{dn}} & \frac{c_{sensor}}{j_{dn}} & \frac{b_{sensor}}{j_{dn}} & \frac{i_{gear}}{j_{dn}} \\ 0 & 0 & 0 & 1 & 0 \\ 0 & -\frac{b_{up}}{j_{up}} + \frac{b_{dn}}{j_{dn}} & -\frac{c_{sensor}}{j_{up}} - \frac{c_{sensor}}{j_{dn}} & -\frac{b_{up}+b_{sensor}}{j_{up}} - \frac{b_{sensor}}{j_{dn}} & -\frac{i_{gear}}{j_{dn}} \\ 0 & 0 & 0 & 0 & -\frac{1}{\tau} \end{bmatrix} \begin{bmatrix} \varphi_{pin} \\ \omega_{pin} \\ \Delta\varphi \\ \dot{\Delta\varphi} \\ T_{mot} \end{bmatrix} + \begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & \frac{1}{j_{dn}} \\ 0 & 0 & 0 \\ 0 & \frac{1}{j_{up}} & -\frac{1}{j_{dn}} \\ \frac{1}{\tau} & 0 & 0 \end{bmatrix} \begin{bmatrix} T_{mot,req} \\ T_{drv} \\ T_{load} \end{bmatrix}$$

$$\begin{bmatrix} \omega_{mot} \\ T_{TSU} \\ T_{mot} \end{bmatrix} = \begin{bmatrix} 0 & i_{gear} & 0 & 0 & 0 \\ 0 & 0 & c_{sensor} & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} \varphi_{pin} \\ \omega_{pin} \\ \Delta\varphi \\ \dot{\Delta\varphi} \\ T_{mot} \end{bmatrix}$$

APPLICATION IN TKP

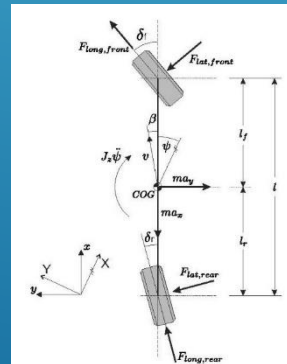
▶ White-box vehicle model identification

- ▶ Linear and nonlinear vehicle model in state-space form. These models are used to simulate dangerous vehicle movements.
- ▶ Autonomous Driving Controllers and algorithms development use these vehicle models.



$$\dot{x} = A(\theta)x + B(\theta)u$$

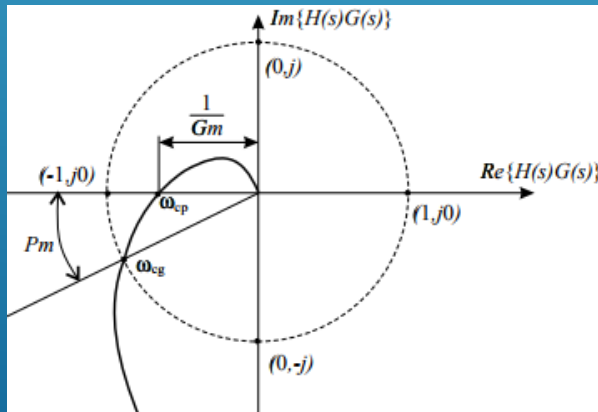
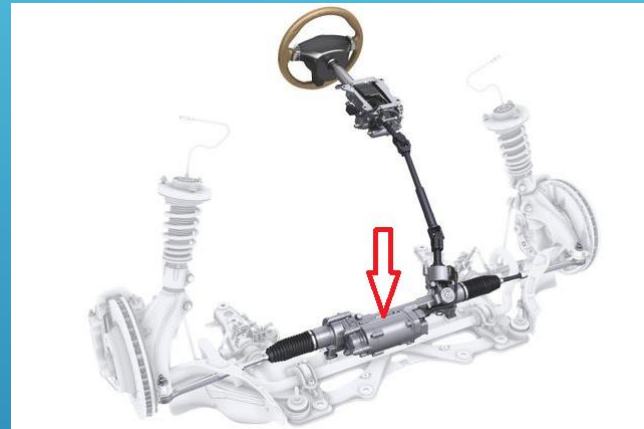
$$y = C(\theta)x + D(\theta)u$$



APPLICATION IN TKP

▶ Black-box vehicle model identification

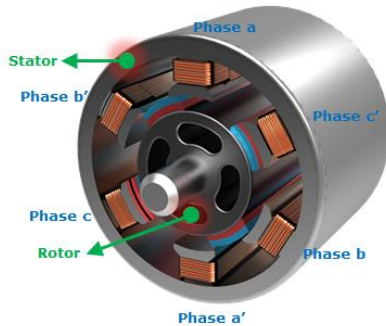
- ▶ Models used for stability analysis in a complete software in the loop environment.
- ▶ Nyquist stability criterion is used to prove the vehicle level stability.



$$\begin{aligned}\dot{x} &= Ax + Bu \\ y &= Cx + Du\end{aligned}$$

APPLICATION IN TKP

- ▶ Permanent magnet synchronous motor parameter identification for motor control purposes:
- ▶ Electro-mechanical steering system model identification.
 - ▶ White-box linear and nonlinear
- ▶ White-box vehicle model identification
- ▶ Black-box vehicle model identification



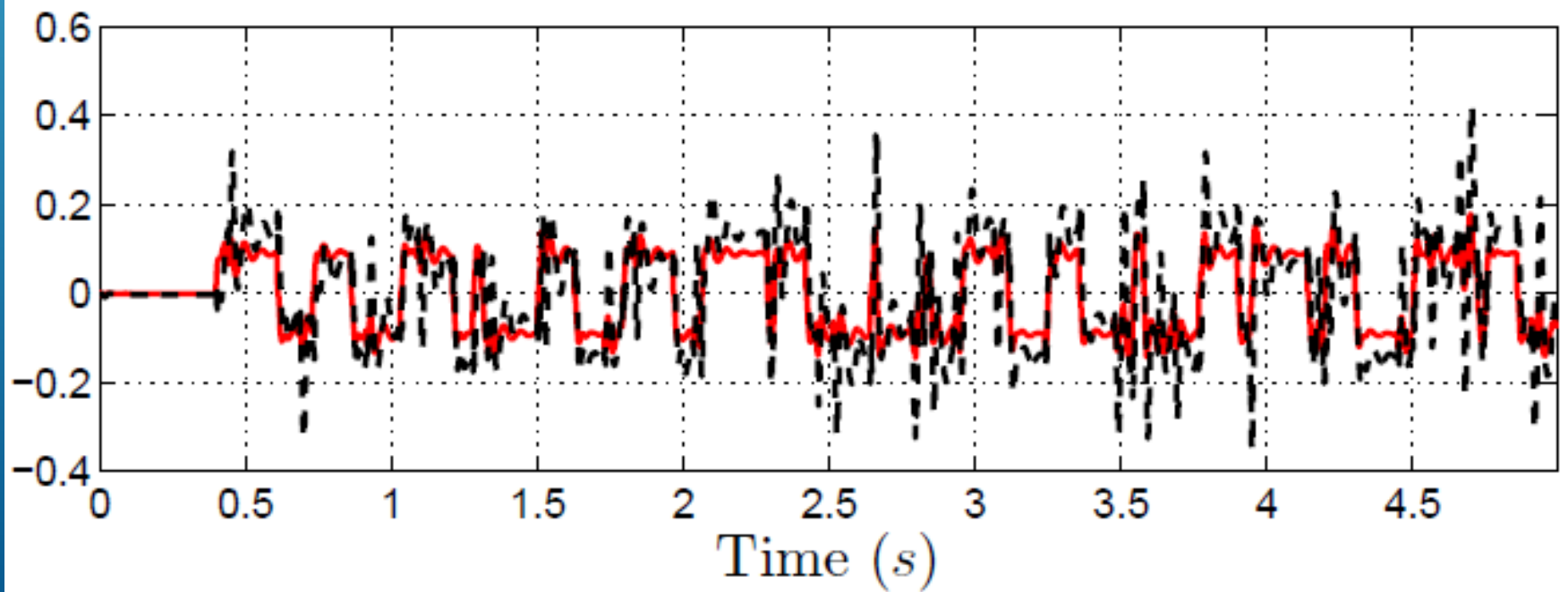
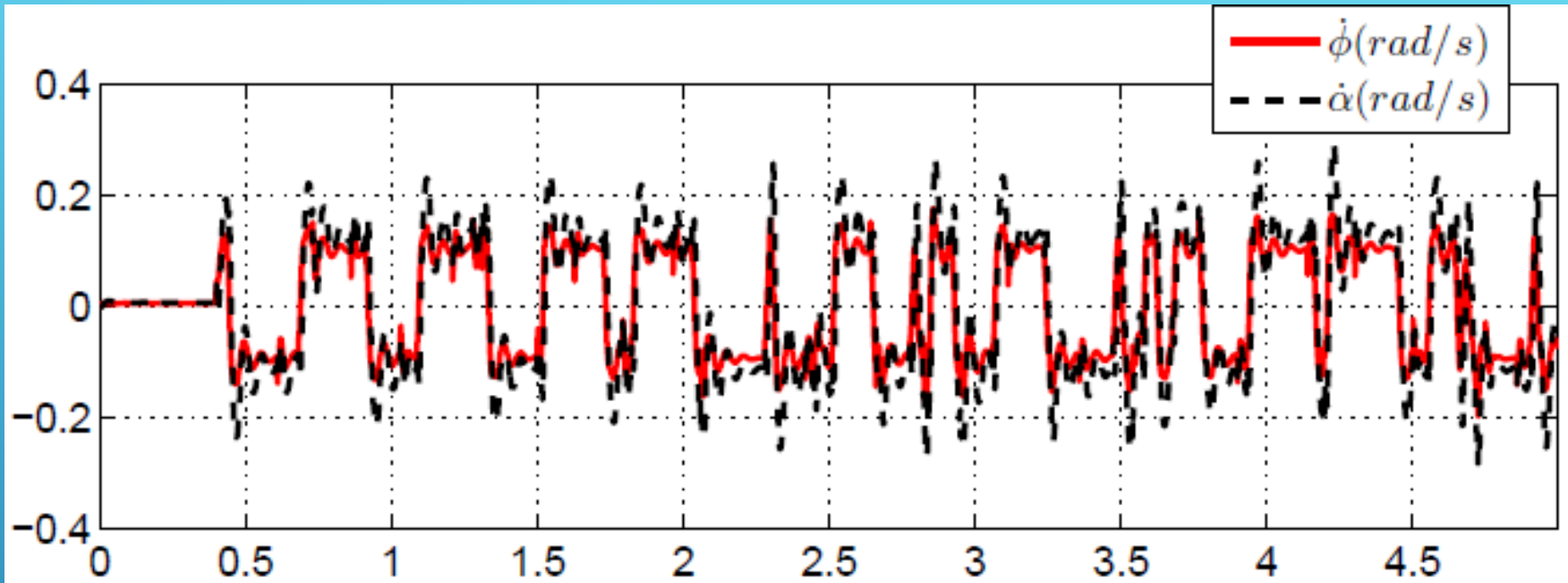
APPLICATION IN TKP

- ▶ Development and maintenance of the numerical optimization tools (bypassing matlab toolboxes)
- ▶ Performing identification, controller design and optimization.
- ▶ Processing the obtained simulation results.
- ▶ Analytical investigation of every aspects of the system:
 - ▶ Feasibility studies for controller and function design.
 - ▶ Mechanical change effect on the system behavior.
- ▶ Seeking for better optimization tools and methods.
- ▶ Model-based controller design for the steering system, autonomous driving.

WHERE A MATEMATICIAN CAN
ENTER INTO THIS PICTURE

THANKS FOR YOUR ATTENTION!





LPV MODELING

Equations of the nonlinear system

$$\begin{aligned} \dot{\mathbf{x}} &= f(\mathbf{x}, \mathbf{u}) \\ \mathbf{y} &= g(\mathbf{x}, \mathbf{u}) \end{aligned}$$

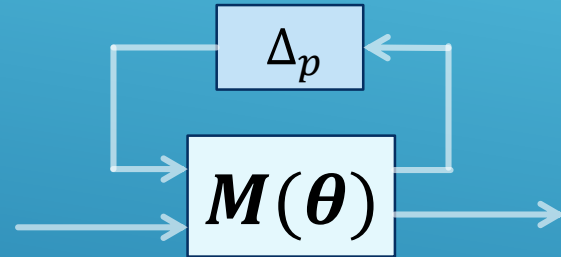


LPV model

$$\begin{aligned} \dot{\mathbf{x}} &= \mathbf{A}_{LPV}(\mathbf{p})\mathbf{x} + \mathbf{B}_{LPV}(\mathbf{p})\mathbf{u} \\ \mathbf{y} &= \mathbf{C}_{LPV}(\mathbf{p})\mathbf{x} + \mathbf{D}_{LPV}(\mathbf{p})\mathbf{u} \end{aligned}$$

Rational LPV model (LPV/LFR)

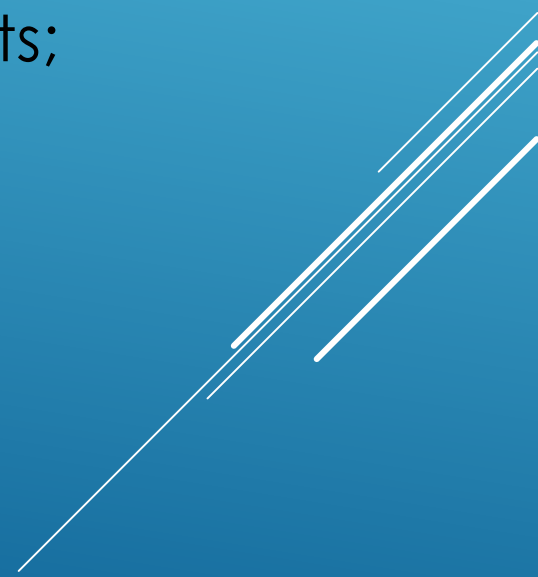
$$\mathbf{M}(\boldsymbol{\theta}) = \begin{bmatrix} \mathbf{D}_{zw} & \mathbf{C}_z & \mathbf{D}_{zu} \\ \mathbf{B}_w & \mathbf{A}_0 & \mathbf{B}_0 \\ \mathbf{D}_{yw} & \mathbf{C}_0 & \mathbf{D}_0 \end{bmatrix}$$



$$\Delta_p = \text{diag}(p_1 I_{r_1}, \dots, p_{n_p} I_{r_{n_p}})$$

$$\begin{bmatrix} \mathbf{A}_{LPV}(\mathbf{p}) & \mathbf{B}_{LPV}(\mathbf{p}) \\ \mathbf{C}_{LPV}(\mathbf{p}) & \mathbf{D}_{LPV}(\mathbf{p}) \end{bmatrix} = \begin{bmatrix} \mathbf{A}_0 & \mathbf{B}_0 \\ \mathbf{C}_0 & \mathbf{D}_0 \end{bmatrix} + \begin{bmatrix} \mathbf{B}_w \\ \mathbf{D}_{yw} \end{bmatrix} \Delta_p (\mathbf{I} - \mathbf{D}_{zw} \Delta_p)^{-1} \begin{bmatrix} \mathbf{C}_z & \mathbf{D}_{zu} \end{bmatrix}$$

LOCAL MODEL ESTIMATION

- 11 operating points are selected: $\left[\frac{\pi}{8} : \frac{\pi}{16} : \frac{6\pi}{8}\right]$;
 - 4x2 MIMO black-box local LTI models are estimated by using a subspace-based technique;
 - The estimated models are validated locally (BFT %);
 - A white-box 2x2 MIMO LPV model is estimated by using a frequency-domain interpolation method based on the 1,3,5,7,9,11th working points;
- 

LPV MODEL IDENTIFICATION

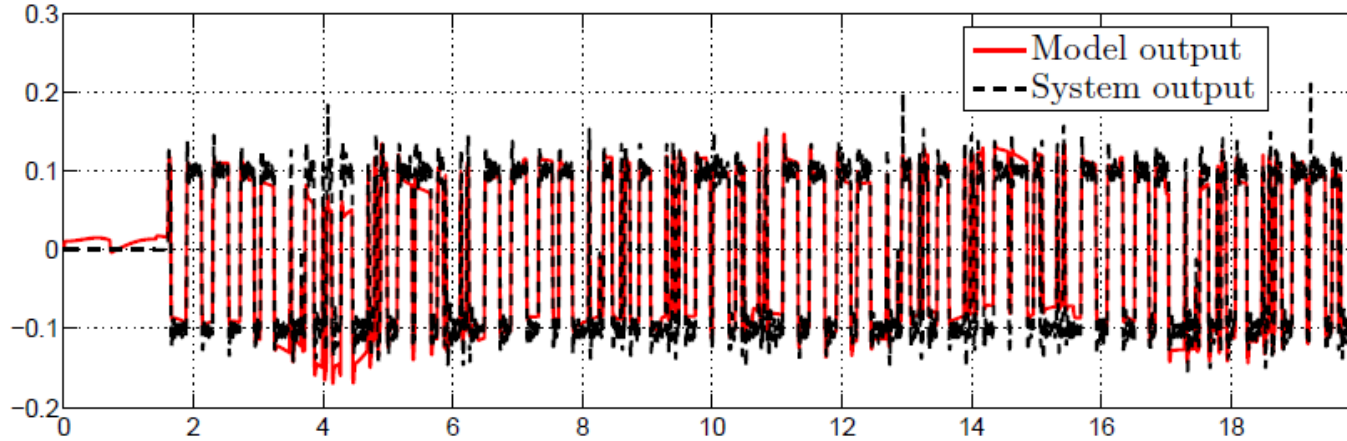
Concatenation of the black-box LTI models.

Forzen LPV model.

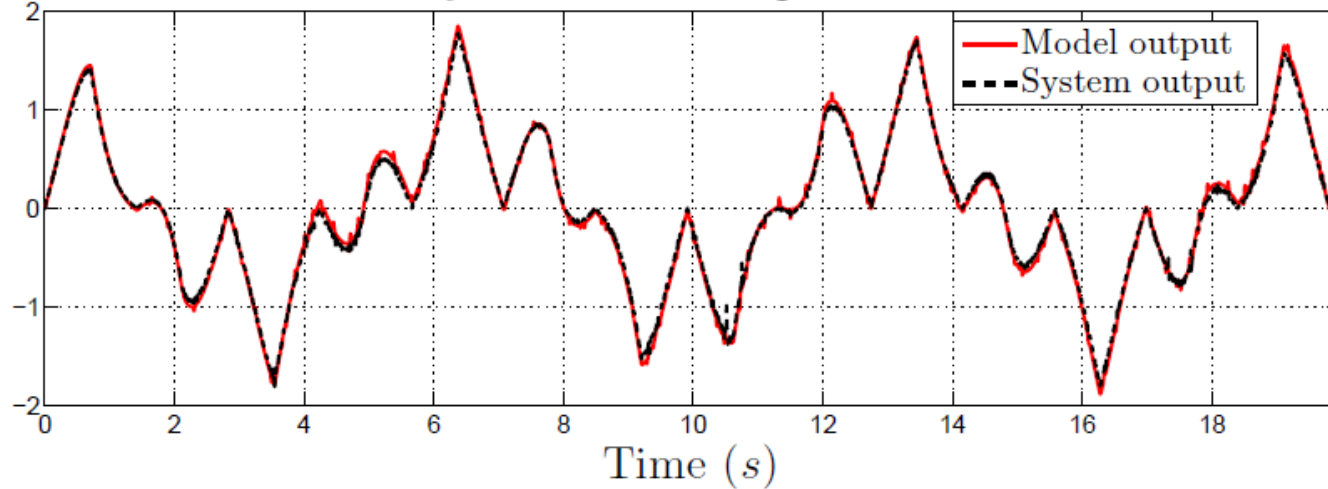
$$\min_{\theta} \sum_{i=1}^N \| \mathbf{G}_{BB}^i(j\omega) - \mathbf{G}_{LPV}(j\omega, \mathbf{p}_i, \theta) \|_{\infty}^2$$

GLOBAL VALIDATION

Real and analytical model outputs - BFT = 73.76 %



Real and analytical model outputs - BFT = 93.22 %



- L. Ljung: System Identification: Theory for the user
- P. Van Overschee, B. de Moor: Subspace identification for linear systems
- R. Tóth: Identification and Modeling of Linear Parameter-Varying Systems
- D. Luenberger: Optimization by vector space methods
- D. Vizer: Application of the H_∞ -norm for the identification of linear time-invariant and linear parameter-varying models, Ph.D thesis.
- K. Pelckmans: Lecture Notes for a course on system identification.
- R. Pintelon, J. Shoukens: System identification: A frequency domain approach

FURTHER READING

THANKS FOR YOUR ATTENTION!

