

```

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fap_n.sm4

MMIX assembly code for low level routines of
fast arbitrary precision arithmetic of natural numbers.

Arbitrary precision natural numbers are represented as a
sequence of words.

A word is an octabyte on MMIX. The most significant word is
on the highest address, and it is always supposed to be non-zero.

Running times here are the running time of the routine,
without the setting up of parameters by callee routine
and the time of the POP instruction for return.

Code length is the number of tetras for the routine, not
counting (one) POP instruction for return.

THE CLASSICAL ALGORITHMS

PREFIX :leading_zeros:

(third-rank candidate to rewrite in assembly)

This simple routine calculate the number of leading zeros of
the nonzero input word.

int leading_zeros(w)
Word   w;      //input word, <>0

Entry:
w      IS      $0      %      the (nonzero) input word
Exit: the number of leading zeros, >=0 and <word_size

Profile:
w=     #fffffffffffffff      #7fffffffffffffff
      4,0,7;0,0              4,0,7;0,0

w=     #3fffffffffffffff      #07fffffffffffffff
      4,0,7;0,0              4,0,7;0,0

w=     #003fffffffffffffff      #00000ffffffffffff
      4,0,7;0,0              4,0,7;0,0

w=     #00000000000003fff
      4,0,7;0,0

PREFIX :trailing_zeros:

```

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(third-rank candidate to rewrite in assembly)

This simple routine calculate the number of trailing zeros of
the nonzero input word.

int trailing_zeros(w)
Word   w;      //input word, <>0

Entry:
w      IS      $0      %      the (nonzero) input word
Exit: the number of trailing zeros, >=0 and <word_size

Profile:
      2 instructions
w=     #fffffffffffffff      #ffffffffffffffe
      2,0,2;0,0              2,0,2;0,0
w=     #fffffffffffffff      #fffffffffffffe0
      2,0,2;0,0              2,0,2;0,0
w=     #fffffffffffffc00      #ffffffff00000
      2,0,2;0,0              2,0,2;0,0
w=     #ffc000000000000
      4,0,7;0,0

PREFIX :ap_l_copy:

(third-rank candidate to rewrite in assembly)

This simple routine copies an arbitrary precision number.

void ap_l_copy(d,s,l)
Word   *d;      // pointer to the LSW of the destination
Word   *s;      // pointer to the LSW of the source
Size   l;      // length of source in words; always nonnegative

Entry:
d      IS      $0      % pointer to the LSW of the destination
s      IS      $1      % pointer to the LSW of the source
l      IS      $2      % length of source in words; always nonnegative.

Exit: -

Profile:
      44 instructions
l=     0              1
      10,0,14;0,1    12,2,16;0,1
l=     2              5

```

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14,4,18;0,1          20,10,24;0,1
l= 10                20
30,20,34;0,1        54,40,58;1,1
l= 50                100
122,100,126;3,1     224,200,238;6,1
l= 200              500
458,400,462;12,1    1134,1000,1138;31,1

PREFIX :ap_l_lsh:

(third-rank candidate to rewrite in assembly)

This simple routine performs a left shift of an arbitrary
precision natural number.  The destination and the source pointer
may be the same.

Size ap_l_lsh(d,s,l,u)

Word  *d;    // pointer to the LSW of the destination
Word  *s;    // pointer to the LSW of the source
Size  l;     // length of source in words; always nonnegative
Word  u;     // number of bits to shift; always nonnegative

Entry:
d      IS      $0      % pointer to the LSW of the destination
s      IS      $1      % pointer to the LSW of the source
l      IS      $2      % length of source in words; always nonnegative
u      IS      $3      % number of bits to shift; always nonnegative

Exit: The length of the result in words

Profile:
26 instructions
l=0,    u=1
2,0,4;0,1
l=1,    u=1
21,2,27;1,3
l=2,    u=1
28,4,34;2,3
l=5,    u=1
49,10,55;5,3
l=10,   u=1
84,20,90;10,3
l=20,   u=1
154,40,160;20,3
l=50,   u=1
364,100,370;50,3
l=100,  u=1
714,200,720;100,3
l=200,  u=1

```

```

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1414,400,1420;200,3
l=500,  u=1
3514,1000,3520;500,3
l=1,    u=100
27,3,33;2,3
l=1,    u=200
33,5,39;4,3
l=1,    u=500
45,9,51;8,3
l=1,    u=1000
69,17,75;16,3
l=1,    u=2000
117,33,123;32,3
l=1,    u=5000
258,80,264;79,3
l=1,    u=10000
492,158,498;157,3
l=1,    u=20000
960,314,966;313,3
l=1,    u=50000
2367,783,2373;782,3

PREFIX :ap_l_rsh:

(third-rank candidate to rewrite in assembly)

This simple routine performs a right shift of an arbitrary
precision natural number.  The destination and the source pointer
may be the same.

Size ap_l_rsh(d,s,l,u)

Word  *d;    // pointer to the LSW of the destination
Word  *s;    // pointer to the LSW of the source
Size  l;     // length of source in words; always nonnegative
Word  u;     // number of bits to shift; always nonnegative

Entry:
d      IS      $0      % pointer to the LSW of the destination
s      IS      $1      % pointer to the LSW of the source
l      IS      $2      % length of source in words; always nonnegative.
u      IS      $3      % number of bits to shift; always nonnegative.

Exit: The length of the result in words

Profile:
26 instructions
l=0,    u=1
7,0,9;0,1
l=1,    u=1

```

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```

16,1,20;1,2
l=2,    u=1
27,4,29;3,1

l=5,    u=1
48,10,50;6,1

l=10,   u=1
83,20,85;11,1

l=20,   u=1
153,40,155;21,1

l=50,   u=1
363,100,365;51,1

l=100,  u=1
713,200,715;101,1

l=200,  u=1
1413,400,1415;201,1

l=500,  u=1
3513,1000,3515;501,1

```

ap_l_addc and ap_l_subc routines

(first-rank candidates to rewrite in assembly)

These simple routines performs addition and subtraction of arbitrary precisions natural numbers having the same length. A carry word (not just one bit!) also added. The destination and the source pointers may be the same

```
Word  ap_l_addc(c,d,s1,s2,l)
```

```
Word  c          // incoming carry
Word  *d         // pointer to the LSW of the destination
Word  *s1        // pointer to the LSW of the first source
Word  *s2        // pointer to the LSW of the second source
Size  l          // length of sources in the words, >=0
```

```
Word  ap_l_subc(c,d,s1,s2,l)
```

```
Word  c          // incoming carry
Word  *d         // pointer to the LSW of the destination
Word  *s1        // pointer to the LSW of the first source
Word  *s2        // pointer to the LSW of the second source
Size  l          // length of sources in the words, >=0
```

Entry:

```

c      IS      $0      % incoming carry
d      IS      $1      % pointer to the LSW of the destination
s1     IS      $2      % pointer to the LSW of the first source
s2     IS      $3      % pointer to the LSW of the second source
l      IS      $4      % length of sources in the words, always nonnegative

```

Exit: the outgoing carry

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```

ap_l_addc
c=1

l=0
1,0,3;0,1

l=1
27,3,31;2,1

l=2
35,6,39;2,1

l=5
59,15,63;2,1

l=10
99,30,103;2,1

l=20
184,60,188;3,1

l=50
434,150,438;5,1

l=100
849,300,853;8,1

l=200
1679,600,1683;14,1

l=500
4174,1500,4178;33,1

ap_l_subc
c=1

l=0
1,0,3;0,1

l=1
27,3,31;2,1

l=2
35,6,39;2,1

l=5
59,15,63;2,1

l=10
99,30,103;2,1

l=20
184,60,188;3,1

l=50
434,150,438;5,1

l=100
849,300,853;8,1

l=200
1679,600,1683;14,1

l=500
4174,1500,4178;33,1

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```

%
% Multiplication and squaring
%
%
% PREFIX :ap_l_mull1c:
%
% (first-rank candidate to rewrite in assembly)
%
% a*m+c is calculated, where a,m and c are words. The LSW of the
% results is put to the place pointed by d. The MSW is the return value.
%
% Word   ap_l_mull1c(c,d,a,m)
%
% Word   c           // incoming carry
% Word   *d          // pointer to the LSW of the destination
% Word   a           // multiplicand
% Word   m           // multiplier
%
% Entry:
%
% c      IS      $0      % incoming carry
% d      IS      $1      % pointer to the LSW of the destination
% a      IS      $2      % multiplicand
% m      IS      $3      % multiplier
%
% Exit: MSW of the result
%
% Profile:
%
% 7 instructions
%
% c=4    a=2    m=3
% 7,1,16;0,0
%
% PREFIX :ap_l_mul21c:
%
% (first-rank candidate to rewrite in assembly)
%
% (s[0]+s[1]*B)*m+c is calculated, where B=2^64.
%
% Word   ap_l_mul21c(c,d,s,m)
%
% Word   c           // incoming carry
% Word   *d          // pointer to the LSW of the destination
% Word   *s          // pointer to the LSW of the multiplicand
% Word   m           // multiplier
%
% Entry:
%
% c      IS      $0      % incoming carry
% d      IS      $1      % pointer to the LSW of the destination
% s      IS      $2      % pointer to the LSW of the multiplicand
% m      IS      $3      % multiplier
%
% Exit: MSW of the result
%
% Profile:

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```

%
% 16 instructions
%
% c=4    s[0]=1  s[1]=2  c=3
% 16,4,34;0,0
%
% PREFIX :ap_l_mul22cc:
%
% (first-rank candidate to rewrite in assembly)
%
% (s[0]+s[1]*B)*(m0+m1*B)+c[0]+c[1]*B is calculated, where B=2^64.
%
% Word   ap_l_mul22cc(c,d,s,m0,m1)
%
% Word   *c          // pointer to the LSW of the two-words incoming carry
% Word   *d          // pointer to the LSW of the destination
% Word   *s          // pointer to the LSW of the multiplicand
% Word   m0         // multiplier LSW
% Word   m1         // multiplier MSW
%
% Entry:
%
% c      IS      $0      % pointer to the LSW of the two-words carry
% d      IS      $1      % pointer to the LSW of the destination
% s      IS      $2      % pointer to the LSW of the destination
% m0     IS      $3      % multiplier LSW
% m1     IS      $4      % multiplier MSW
%
% Exit: c[0] and c[1] is set
%
% Profile:
%
% 40 instructions
%
% c[0]=1001 c[1]=1002 s[0]=1 s[1]=2 m0=3 m1=4
% 40,8,76;0,0
%
% PREFIX :ap_l_mull1addc:
%
% (first-rank candidate to rewrite in assembly)
%
% a*b+c+d[0] is calculated, where a,b,c and d[0] are words.
% The LSW of the result replace d[0] and the MSW of the result
% is the return value.
%
% Word   ap_l_mull1addc(c,d,a,m)
%
% Word   c           // incoming carry
% Word   *d          // pointer to the LSW of the source/destination
% Word   a           // multiplicand
% Word   m           // multiplier
%
% Entry:
%
% c      IS      $0      % third operand
% d      IS      $1      % pointer to the LSW of the destination/source
% a      IS      $2      % first operand
% b      IS      $3      % second operand

```

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```

Exit: MSW of the result

```

```

Profile:

```

```

c=4      [d]=1   a=2     b=3
12,2,21;0,0

```

```

PREFIX :ap_l_mul21addc:

```

```

(first-rank candidate to rewrite in assembly)

```

```

(s[0]+s[1]*B)*m+c+d[0]+d[1]*B is calculated, where B=2^64
and s[0], s[1], m, c, d[0] and d[1] are words.
The result replace d[0], d[1] and the MSW of the result is
the return value.

```

```

Word      ap_l_mul21addc(c,d,s,m)

```

```

Word      c          // incoming carry
Word      *d         // pointer to the LSW of the source/destination
Word      *s         // pointer to the LSW of multiplicand
Word      m          // multiplier

```

```

Entry:

```

```

C          IS          $0          % carry
d          IS          $1          % pointer to the LSW of the destination/source
s          IS          $2          % pointer to the LSW of multiplicand
m          IS          $3          % multiplier

```

```

Exit: MSW of the result

```

```

Profile:

```

```

26 instructions

```

```

c=4 d[0]=1 d[1]=2 s[0]=1001 s[1]=1002 m=3
26,6,44;0,0

```

```

PREFIX :ap_l_mul22addcc:

```

```

(first-rank candidate to rewrite in assembly)

```

```

(s[0]+s[1]*B)*(m0+m1*B)+c[0]+d[0]+(c[1]+d[1])*B is calculated,
where B=2^64 and s[0], s[1], m0, m1, c[0], c[1], d[0] and d[1]
are words. The result replace d[0], d[1] and the MSW of the result is
the return value.

```

```

Void      ap_l_mul22addc(c,d,s,m0,m1)

```

```

Word      *c         // pointer to the LSW of the carries c[0], c[1]
Word      *d         // pointer to the LSW of the source/destination
Word      *s         // pointer to the LSW of multiplicand
Word      m0        // multiplier, LSW
Word      m1        // multiplier, MSW

```

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```

Entry:

```

```

c          IS          $0          % pointer to the LSW of the carries c[0], c[1]
d          IS          $1          % pointer to the LSW of the destination/source
s          IS          $2          % pointer to the LSW of multiplicand
m0         IS          $3          % multiplier, LSW
m1         IS          $4          % multiplier, MSW

```

```

Exit: c[0], c[1] are set

```

```

Profile:

```

```

48 instructions

```

```

c[0]=2001 c[1]=2002 d[0]=1 d[1]=2 s[0]=1001 s[1]=1002 m0=3 m1=4
48,10,84;0,0

```

```

PREFIX :ap_l_mullc:

```

```

(second-rank candidate to rewrite in assembly)

```

```

This routine multiplies an arbitrary precision natural number
pointed by s with a word m and adds a carry word c. The result
is stored at place pointed by d. The length of d and s is l>0.
The new carry is returned.

```

```

Word      ap_l_mull(c,d,s,m,l)

```

```

Word      c          // carry
Word      *d         // pointer to the LSW of destination
Word      *s         // pointer to the LSW of multiplicand
Word      m          // multiplier
Size      l          // length of source and destination in words

```

```

Entry:

```

```

c          IS          $0          % carry word
d          IS          $1          % pointer to LSW of destination
s          IS          $2          % pointer to LSW of source
m          IS          $3          % multiplier
l          IS          $4          % length of source and destination in words

```

```

Exit: MSW of the result

```

```

Profile:

```

```

14 instructions

```

```

c=0,      m=0

```

```

l=1
14,2,25;0,1

```

```

l=2
24,4,44;1,1

```

```

l=5

```

```

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54,10,101;4,1
l=10
104,20,196;9,1

l=20
204,40,386;19,1

l=50
504,100,956;49,1

l=100
1004,200,1906;99,1

l=200
2004,400,3806;199,1

l=500
5004,1000,9506;499,1

c=0,      m=#fffffffffffffff

l=1
14,2,25;0,1

l=2
24,4,44;1,1

l=5
54,10,101;4,1

l=10
104,20,196;9,1

l=20
204,40,386;19,1

l=50
504,100,956;49,1

l=100
1004,200,1906;99,1

l=200
2004,400,3806;199,1

l=500
5004,1000,9506;499,1

PREFIX :ap_l_mul2:

(second-rank candidate to rewrite in assembly)

This routine multiplies an arbitrary precision natural number
pointed by s with a two-word number m0+m1*B, where B=2^64.
The result is stored at place pointed by d.
The length of d and s is l>1.
The MSW is returned, the second MSW is stored.
The new carry is returned.

Word      ap_l_mul2(d,s,m0,m1,l)

Word      *d      // pointer to the LSW of destination
Word      *s      // pointer to the LSW of multiplicand
    
```

```

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%      Word      m0      // multiplier, LSW
%      Word      m1      // multiplier, MSW
%      Size      1      // length of source and destination in words

Entry:
d      IS      $0      % pointer to LSW of destination
s      IS      $1      % pointer to LSW of source
m0     IS      $2      % multiplier, LSW
m1     IS      $3      % multiplier, MSW
l      IS      $4      % length of source and destination in words

Exit: MSW of the result

Profile:

simple version:

37 instructions

m0=3    m1=4

l=2
37,5,75;0,1

l=5
94,11,184;3,1

l=10
189,21,371;8,1

l=20
379,41,741;18,1

l=50
949,101,1851;48,1

l=100
1899,201,3701;98,1

l=200
3799,401,7401;198,1

l=500
9499,1001,18501;498,1

m0=3    m1=#fffffffffffffff

l=2
37,5,75;0,1

l=5
94,11,184;3,1

l=10
189,21,371;8,1

l=20
379,41,741;18,1

l=50
949,101,1851;48,1

l=100
1899,201,3701;98,1
    
```

```

l=200
3799,401,7401;198,1

l=500
9499,1001,18506;498,1

PREFIX :ap_l_mulladdc:

(second-rank candidate to rewrite in assembly)

This routine multiplies an arbitrary precision natural number
pointed by s with a word m and adds a carry word c to the
product. The result is added to the destination pointed by d.
The length of d and s is l, may be 0.
The new carry is returned.

Word    ap_l_mulladdc(c,d,s,m,l)

Word    c        // incoming carry
Word    *d       // pointer to the LSW of destination
Word    *s       // pointer to the LSW of multiplicand
Word    m        // multiplier
Size    l        // length of source and destination in words

Entry:

C      IS      $0      % carry word
D      IS      $1      % pointer to LSW of destination
S      IS      $2      % pointer to LSW of source
M      IS      $3      % multiplier
l      IS      $4      % length of source and destination in words

Exit: MSW of the result

Profile:

20 instructions

c=0,    m=0

l=0
1,0,3;0,1

l=1
21,3,32;1,1

l=2
35,6,55;2,1

l=5
77,15,124;5,1

l=10
147,30,239;10,1

l=20
287,60,469;20,1

l=50
707,150,1159;50,1
    
```

```

l=100
1407,300,2307;100,1

l=200
2807,600,4607;200,1

l=500
7007,1500,11507;500,1

c=0,    m=#fffffffffffffff

l=0
1,0,3;0,1

l=1
21,3,32;1,1

l=2
35,6,55;2,1

l=5
77,15,124;5,1

l=10
147,30,239;10,1

l=20
287,60,469;20,1

l=50
707,150,1159;50,1

l=100
1407,300,2307;100,1

l=200
2807,600,4607;200,1

l=500
7007,1500,11507;500,1

PREFIX :ap_l_mul2add:

(second-rank candidate to rewrite in assembly)

This routine multiplies an arbitrary precision natural number
pointed by s with a two-word number m0+m1*B, where
B=2^64, and adds a carry word c.
The result is stored at place pointed by d.
The length of d and s is l>1.
The MSW is returned, the second MSW is stored.

Word    ap_l_mul2add(d,s,m0,m1,l)

Word    *d       // pointer to the LSW of destination
Word    *s       // pointer to the LSW of multiplicand
Word    m0       // multiplier, LSW
Word    m1       // multiplier, MSW
Size    l        // length of source and destination in words

Entry:
    
```

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```

d      IS      $0      % pointer to LSW of destination
s      IS      $1      % pointer to LSW of source
m0     IS      $2      % multiplier
m1     IS      $3      % multiplier
l      IS      $4      % length of source and destination in words

```

```

% Exit: MSW of the result

```

```

% Profile:

```

```

46 instructions

```

```

m0=3    m1=4    s[0]=1 ...    d[1]=1001 ...

```

```

l=2
46,7,84;0,1

```

```

l=5
115,16,207;3,1

```

```

l=10
230,31,412;8,1

```

```

l=20
460,61,822;18,1

```

```

l=50
1150,151,2052;48,1

```

```

l=100
2300,301,4102;98,1

```

```

l=200
4600,601,8202;198,1

```

```

l=500
11500,1501,20502;498,1

```

```

m0=3    m1=#fffffffffffffffff    s[0]=1 ...    d[1]=1001 ...

```

```

l=2
46,7,84;0,1

```

```

l=5
115,16,207;3,1

```

```

l=10
230,31,412;8,1

```

```

l=20
460,61,822;18,1

```

```

l=50
1150,151,2052;48,1

```

```

l=100
2300,301,4102;98,1

```

```

l=200
4600,601,8202;198,1

```

```

l=500
11500,1501,20502;498,1

```

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```

% PREFIX :ap_l_mul_class:

```

```

% (third-rank candidate to rewrite in assembly)

```

```

% This routine multiplies an arbitrary precision natural number
% pointed by s1 with an other arbitrary precision number pointed
% by s2. The numbers has length l1 and l2, respectively, where
% l1>=l2>0 is supposed. The least significant l1+l2-1 word of
% the result is put to the place pointed by d, the MSW is the
% return value.

```

```

% Word    ap_l_mul_class(d,s1,s2,l1,l2)

```

```

% Word    *d        // pointer to the LSW of destination
% Word    *s1        // pointer to the LSW of multiplicand
% Word    *s2        // pointer to the LSW of multiplier
% Size    l1         // length of multiplicand
% Size    l2         // length of multiplier

```

```

% Entry:

```

```

d      IS      $0      % pointer to LSW of destination
s1     IS      $1      % pointer to LSW of first source
s2     IS      $2      % pointer to LSW of second source
l1     IS      $3      % length of first source in words
l2     IS      $4      % length of second source in words

```

```

% Exit: MSW of the result

```

```

% Profile:

```

```

116 instructions

```

```

l=11=12

```

```

l=1
26,3,38;1,2

```

```

l=2
46,7,88;0,3

```

```

l=3
117,20,204;5,3

```

```

l=4
179,27,331;5,4

```

```

l=5
301,49,534;13,4

```

```

l=6
404,59,738;14,5

```

```

l=7
577,90,1028;25,5

```

```

l=8
721,103,1309;27,6

```

```

l=9
945,143,1686;41,6

```

```

l=10
1130,159,2044;44,7

```


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```

l=11
1405,208,2508;61,7

l=12
1631,227,2943;65,8

l=13
1957,285,3494;85,8

l=14
2224,307,4006;90,9

l=15
2601,374,4644;113,9

l=16
2909,399,5233;119,10

PREFIX :ap_l_sqr1:

(first-rank candidate to rewrite in assembly)

a*a is calculated, where a is a word. The LSW of the
results is put to the place pointed by p, the MSW is the return value.

Word   ap_l_sqr1(d,a)

Word   *d       // pointer to the LSW of destination
Word   a        // input word

Entry:
d      IS      $0      % pointer to the LSW of the destination
a      IS      $1      % operand

Exit: MSW of the result

Profile:

3 instruction

a=2    c=3    [d]=1
3,1,12;0,0

PREFIX :ap_l_sqr1addc:

(first-rank candidate to rewrite in assembly)

a*a+c+d[0] is calculated, where a,c and d[0] are words.
The LSW of the result replace d[0] and the MSW of the result
the return value.

Word   ap_l_sqr1addc(c,d,a)

Word   c        // carry
Word   *d       // pointer to the LSW of source/destination

```

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```

Word   a        // input word

Entry:
c      IS      $0      % carry
d      IS      $1      % pointer to the LSW of the destination/source
a      IS      $2      % operand

Exit: MSW of the result

Profile:

12 instruction

c=3    d[0]=1  a=2
12,2,21;0,0

PREFIX :ap_l_sqr2:

(first-rank candidate to rewrite in assembly)

(a0+a1*B)^2 is calculated, where B=2^64

Word   ap_l_sqr2(d,a0,a1)

Word   *d       // pointer to the LSW of source/destination
Word   a0      // input LSW
Word   a1      // input MSW

Entry:
d      IS      $0      % pointer to the LSW of the destination
a0     IS      $1      % operand LSW
a1     IS      $2      % operand MSW

Exit: MSW of the result

Profile:

25 instructions

a0=2   a1=3
25,3,52;0,0

PREFIX :ap_l_sqr2addcc:

(first-rank candidate to rewrite in assembly)

(a0+a1*B)^2+c[0]+c[1]*B+d[0]+d[1]*B is calculated, where B=2^64

Word   ap_l_sqr2addcc(c,d,a0,a1)

Word   *c       // pointer to the two-word in/out carry

```

```

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%      Word      *d      // pointer to the LSW of source/destination
%      Word      a0      // input LSW
%      Word      a1      // input MSW
%
% Entry:
%
C      IS      $0      % pointer to the LSW of the carry
d      IS      $1      % pointer to the LSW of the destination/source
a0     IS      $2      % operand LSW
a1     IS      $3      % operand MSW
%
% Exit: c[0], c[1] set
%
% Profile:
%
%      44 instructions
%
%      c[0]=1 c[1]=2 d[0]=1001 d[1]=1002 a0=2 a1=3
%      44,8,71;0,0
%
%
% PREFIX :ap_l_sqr_class:
%
% (third-rank candidate to rewrite in assembly)
%
% This routine squares an arbitrary precision natural number
% pointed by s. The numbers has length l, where
% l>0 is supposed. The least significant 2*l-1 word of
% the result is put to the place pointed by d, the MSW is the
% return value.
%
% Word      ap_l_sqr_class(d,s,l)
%
% Word      *c      // pointer to the LSW of destination
% Word      *d      // pointer to the LSW of source
% Size      l      // length of source in words, always positive
%
% Entry:
%
d      IS      $0      % pointer to LSW of destination
s      IS      $1      % pointer to LSW of source
l      IS      $2      % length of source in words, always positive
%
% Exit: MSW of the result
%
% Profile:
%
%      162 instructions
%
%      treshold=2
%
%      l=1
%      12,2,23;1,1
%
%      l=2
%      34,5,63;2,1
%
%      l=3
%      108,23,170;3,4

```

```

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%
%      l=4
%      155,31,255;3,5
%
%      l=5
%      244,49,389;9,5
%
%      l=6
%      309,57,510;9,6
%
%      l=7
%      428,81,692;17,6
%
%      l=8
%      511,89,849;17,7
%
%      l=9
%      660,119,1079;27,7
%
%      l=10
%      761,127,1272;27,8
%
%      l=11
%      940,163,1550;39,8
%
%      l=12
%      1059,171,1779;39,9
%
%      l=13
%      1268,213,2105;53,9
%
%      l=14
%      1406,221,2370;53,10
%
%      l=15
%      1644,269,2744;69,10
%
%      l=16
%      1799,277,3045;69,11
%
%
% PREFIX :ap_l_mullsubc:
%
% (first-rank candidate to rewrite in assembly)
%
% d[0]-c-a*b is calculated
%
% Word      ap_l_mullsubc(d,s,a,m)
%
% Word      c      // carry
% Word      *d      // pointer to the LSW of source/destination
% Word      a      // multiplicand
% Word      m      // multiplier
%
% Entry:
%
C      IS      $0      % carry
d      IS      $1      % pointer to the LSW of the destination/source
a      IS      $2      % multiplicand
m      IS      $3      % multiplier
%
% Exit: MSW of the result; i.e. -2^64*MSW+d[0] is the result
%
% Profile:

```

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```

12 instructions

c=4      d[0]=1  a=2      m=3
12,2,21;0,0

PREFIX :ap_l_mul21subc:
(first-rank candidate to rewrite in assembly)
d[0]+d[1]*B-(s[0]+s[1]*B)*m-c is calculated, where B=2^64

Word    ap_l_mul21subc(c,d,s,m)

Word    c          // carry
Word    *d         // pointer to the LSW of source/destination
Word    *s         // pointer to the LSW of multiplicand
Word    m          // multiplier

Entry:
C       IS        $0        % carry
d       IS        $1        % pointer to the LSW of the destination/source
s       IS        $2        % pointer to the LSW of multiplicand
m       IS        $3        % multiplier

Exit: MSW of the result; i.e. -2^128*MSW+d[0]+d[1]*B is the result

Profile:
26 instructions

c=4 d[0]=1 d[1]=2 s[0]=1001 s[0]=1002 m=3
26,6,44;0,0

PREFIX :ap_l_mul22subcc:
(first-rank candidate to rewrite in assembly)
d[0]+d[1])*B-(s[0]+s[1]*B)*(m0+m1*B)-c[0]-c[1]*B is calculated,
where B=2^64

Word    ap_l_mul22subcc(c,d,s,m0,m1)

Word    c          // carry
Word    *d         // pointer to the LSW of source/destination
Word    *s         // pointer to the LSW of multiplicand
Word    m0         // multiplier, LSW
Word    m1         // multiplier, LSW

Entry:
C       IS        $0        % pointer to the LSW of the carries c[0], c[1]
d       IS        $1        % pointer to the LSW of the destination/source
s       IS        $2        % pointer to the LSW of multiplicand

```

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```

m0      IS        $3        % multiplier, LSW
m1      IS        $4        % multiplier, MSW

Exit: c[0], c[1] are set; i.e., the result is
(c[0]+c[1]*B)*B^2-d[0]-d[1]*B

Profile:
48 instructions

c[0]=2001 c[1]=2002 d[0]=1 d[1]=2 s[0]=1001 s[1]=1002 m0=3 m1=4
48,10,84;0,0

PREFIX :ap_l_mullsubc:
(second-rank candidate to rewrite in assembly)

This routine multiplies an arbitrary precision natural number
pointed by s with a word m and adds a carry word c to the
product. The result is added to the destination pointed by d.
The length of d and s is l. The new carry is returned.

Word    ap_l_mullsubc(c,d,s,m0,m1)

Word    c          // carry
Word    *d         // pointer to the LSW of source/destination
Word    *s         // pointer to the LSW of multiplicand
Word    m          // multiplier
Size    l          // length of source and destination in words, >0

Entry:
C       IS        $0        % carry word
d       IS        $1        % pointer to LSW of destination
s       IS        $2        % pointer to LSW of source
m       IS        $3        % multiplier
l       IS        $4        % length of source and destination in words, >0

Exit: MSW of the result

Profile:
20 instructions

c=0,      m=0

l=1
20,3,31;0,1

l=2
34,6,54;1,1

l=5
76,15,123;4,1

l=10
146,30,238;9,1

l=20

```

```

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286,60,468;19,1
l=50
706,150,1158;49,1
l=100
1406,300,2306;99,1
l=200
2806,600,4606;199,1
l=500
7006,1500,11506;499,1
c=0,      m=#fffffffffffffff
l=1
20,3,31;0,1
l=2
34,6,54;1,1
l=5
76,15,123;4,1
l=10
146,30,238;9,1
l=20
286,60,468;19,1
l=50
706,150,1158;49,1
l=100
1406,300,2306;99,1
l=200
2806,600,4606;199,1
l=500
7006,1500,11506;499,1
PREFIX :ap_l_mul2sub:
(second-rank candidate to rewrite in assembly)
This routine multiplies an arbitrary precision natural number
pointed by s with a two-word number m0+m1*B, where
B=2^64, and adds a carry word c.
The result is stored at place pointed by d.
The length of d and s is l>1.
The MSW is returned, the second MSW is stored.
Word   ap_l_mul2sub(d,s,m0,m1,l)
Word   *d      // pointer to the LSW of source/destination
Word   *s      // pointer to the LSW of multiplicand
Word   m0      // multiplier, LSW
Word   m1      // multiplier, MSW
Size   l      // length of source and destination in words, >0

```

```

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% Entry:
d      IS      $0      % pointer to LSW of destination
s      IS      $1      % pointer to LSW of source
m0     IS      $2      % multiplier
m1     IS      $3      % multiplier
l      IS      $4      % length of source and destination in words
% Exit: MSW of the result
% Profile:
47 instructions
m0=3   m1=4   s[0]=1 ...   d[1]=1001 ...
l=2
47,7,85;0,1
l=5
116,16,208;3,1
l=10
231,31,413;8,1
l=20
461,61,823;18,1
l=50
1151,151,2053;48,1
l=100
2301,301,4103;98,1
l=200
4601,601,8203;198,1
l=500
11501,1501,20503;498,1
m0=3   m1=#fffffffffffffff   s[0]=1 ...   d[1]=1001 ...
l=2
47,7,85;0,1
l=5
116,16,208;3,1
l=10
231,31,413;8,1
l=20
461,61,823;18,1
l=50
1151,151,2053;48,1
l=100
2301,301,4103;98,1
l=200
4601,601,8203;198,1
l=500
11501,1501,20503;498,1

```

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```

%
%
%
PREFIX :ap_l_div21:
%
%
% (first-rank candidate to rewrite in assembly)
%
% The quotient (a[0]+ah*B)/b and the remainder are calculated; B=2^64.
% We suppose that bl<>0, and the quotient is one word.
%
% Word    ap_l_div21(ah,a,b)
%
% Word    ah        // MSW of dividend
% Word    *a        // pointer to the LSW of source/destination
% Word    b         // divisor
%
% Entry:
%
ah      IS      $0      % MSW of dividend
a       IS      $1      % pointer to the LSW of source/destination
b       IS      $2      % divisor
%
% Exit: quotient; remainder in a[0]
%
% Profile:
%
% 5 instructions
%
% b=3      a[0]=1  ah=2
% 5,2,64;0,0
%
%
% PREFIX :ap_l_div21r:
%
% (first-rank candidate to rewrite in assembly)
%
% the quotient (a[0]+ah*B)/b and the remainder are calculated; B=2^64.
% WE SUPPOSE THAT b>=B/2 and the quotient is one word.
%
% Word    ap_l_div21r(ah,a,b,rec)
%
% Word    ah        // MSW of dividend
% Word    *a        // pointer to the LSW of source/destination
% Word    b         // divisor, b>=B/2=2^63
% Word    rec       // reciprocial: floor((2^128-1)/b-B)
%
% Entry:
%
ah      IS      $0      % MSW of dividend
a       IS      $1      % pointer to the LSW of source/destination
b       IS      $2      % divisor, b>=B/2=2^63
rec     IS      $3      % reciprocial: floor((2^128-1)/b-B)
%
% Exit: quotient; remainder in a[0]
%
% Profile:

```

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```

%
% 30 instructions
%
% b=#c000000000000000  a[0]=1  ah=2  rec=#5555555555555555
% 30,2,48;0,0
%
%
% PREFIX :quo32:
%
% (first-rank candidate to rewrite in assembly)
%
% The quotient (as[0]+as[1]*B+as[2]*B^2)/(b0+b1*B)
% is calculated, where the dividend is
% (a[-2]+a[-1]*B+a[0]*B^2+ah*B^3)>>(64-lz), and B=2^64.
% We suppose that bl>=B/2, and the quotient is two words.
%
% Word    quo32(ah,a,b,lz)
%
% Word    ah        // MSW of unshifted dividend
% Word    *a        // pointer to the second MSW of the unshifted dividend
% Word    *b        // pointer to the LSW of the shifted divisor
% Word    lz        // leading zeros of the unshifted divisor
%
% Entry:
%
ah      IS      $0      % MSW of unshifted dividend
a       IS      $1      % pointer to the second MSW of the unshifted dividend
b       IS      $2      % pointer to the LSW of the shifted divisor
lz      IS      $3      % leading zeros of the unshifted divisor
%
% Exit: quotient MSW
%
% Profile:
%
% 52 instructions
%
% b[1]=#c000000000000000  b[0]=0
% ah=2 a[0]=3 a[-1]=2 a[-2]=1 lz=62
% 40,7,117;1,0
%
%
% PREFIX :quo32r:
%
% (first-rank candidate to rewrite in assembly)
%
% The quotient (as[0]+as[1]*B+as[2]*B^2)/(b0+b1*B)
% is calculated, where the dividend is
% (a[-2]+a[-1]*B+a[0]*B^2+ah*B^3)>>(64-lz), and B=2^64.
% WE SUPPOSE THAT bl>=B/2, and the quotient is two words.
% Reciprocal floor((2^128-1)/b1-B) is used.
%
% Word    quo32r(ah,a,b,lz,rec)
%
% Word    ah        // MSW of unshifted dividend
% Word    *a        // pointer to the second MSW of the unshifted dividend
% Word    *b        // pointer to the LSW of the shifted divisor
% Word    lz        // leading zeros of the unshifted divisor
% Word    rec       // reciprocial: floor((2^128-1)/b1-B),

```

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```

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%
%           where b1>=B/2=2^63
%
% Entry:
%
ah      IS      $0      % MSW of unshifted dividend
a       IS      $1      % pointer to the second MSW of the unshifted dividend
b       IS      $2      % pointer to the LSW of the shifted divisor
lz      IS      $3      % leading zeros of the unshifted divisor
rec     IS      $4      % reciprocal: floor((2^128-1)/b1-B),
%           where b1>=B/2=2^63
%
% Exit: quotient MSW
%
% Profile:
%
%       76 instructions
%
%       b[1]=#c000000000000000 b[0]=0 lz=62 rec=#5555555555555555
%       ah=2 a[0]=3 a[-1]=2 a[-2]=1
%       64,6,103;0,1
%
%
% PREFIX :ap_l_div42:
%
% (second-rank candidate to rewrite in assembly)
%
% the quotient (a[0]+a[1]*B+a[2]*B^2+ah*B^3)/(b0+b1*B)
% and the remainder are calculated; B=2^64.
% We suppose that b1*B+b0<>0, and the quotient is two words.
%
% Word   ap_l_div42(ah,a,b0,b1)
%
% Word   ah      // MSW of dividend
% Word   *a      // pointer to the LSW of source/destination
% Word   b0      // divisor LSW
% Word   b1      // divisor MSW
%
% Entry:
%
ah      IS      $0      % MSW of dividend
a       IS      $1      % pointer to the LSW of source/destination
b0      IS      $2      % divisor LSW
b1      IS      $3      % divisor MSW
%
% Exit: quotient MSW; remainder in a[0], a[1]; quotient LSW in a[2]
%
% Profile:
%
%       120 instructions
%
%       ah=0 a[0]=1 a[1]=2 a[2]=3 b0=2 b1=3
%       73,6,234;1,2
%
%
% PREFIX :ap_l_div42r:
%
% (second-rank candidate to rewrite in assembly)
%
% The quotient (a[0]+a[1]*B+a[2]*B^2+ah*B^3)/(b0+b1*B)

```

```

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%
% and the remainder are calculated; B=2^64.
% WE SUPPOSE THAT b1>=B/2, and the quotient is two words.
%
%
% Word   ap_l_div42r(ah,a,b0,b1,rec)
%
% Word   ah      // MSW of unshifted dividend
% Word   *a      // pointer to the second MSW of the unshifted dividend
% Word   b0      // LSW of the divisor
% Word   b1      // MSW of the divisor
% Word   rec     // reciprocal: floor((2^128-1)/b1-B),
%           where b1>=B/2=2^63
%
% Entry:
%
ah      IS      $0      % MSW of dividend
a       IS      $1      % pointer to the LSW of source/destination
b0      IS      $2      % divisor LSW
b1      IS      $3      % divisor MSW
rec     IS      $4      % reciprocal: floor((2^128-1)/b1-B),
%           where b1>=B/2=2^63
%
% Exit: quotient MSW; remainder in a[0], a[1]; quotient LSW in a[2]
%
% Profile:
%
%       simple version:
%
%       140 instructions
%
%       ah=0 a[0]=1 a[1]=2 a[2]=3
%       b0=2 b1=#c000000000000000 rec=5555555555555555
%       102,6,178;0,2
%
%
% PREFIX :ap_l_div42rr:
%
% (second-rank candidate to rewrite in assembly)
%
% The quotient (a[0]+a[1]*B+a[2]*B^2+ah*B^3)/(b0+b1*B)
% and the remainder are calculated; B=2^64.
% WE SUPPOSE THAT b1>=B/2, and the quotient is two words.
%
% Word   ap_l_div42rr(ah,a,b0,b1,rec0,rec1)
%
% Word   ah      // MSW of unshifted dividend
% Word   *a      // pointer to the second MSW of the unshifted dividend
% Word   b0      // LSW of the divisor
% Word   b1      // MSW of the divisor
% Word   rec0    // reciprocal LSW
% Word   rec1    // reciprocal MSW:
%
%       rec0+rec1*B=floor((2^256-1)/(b1*B+b0)-B^2), where b1>=B/2=2^63
%
% Entry:
%
ah      IS      $0      % MSW of dividend
a       IS      $1      % pointer to the LSW of source/destination
b0      IS      $2      % divisor LSW
b1      IS      $3      % divisor MSW
rec0    IS      $4      % reciprocal LSW

```

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```

rec1 IS $5 % reciprocal MSW:
%
% rec0+rec1*B=floor((2^256-1)/(b1*B+b0)-B^2), where b1>=B/2=2^63
%
% Exit: quotient MSW; remainder in a[0], a[1]; quotient LSW in a[2]
%
% Profile:
%
% 102 instructions
%
% ah=0 a[0]=1 a[1]=2 a[2]=3 b0=0 b1=#c000000000000000
% rec0=#5555555555555555 rec1=#5555555555555555
% 104,6,176;0,0
%
%
% PREFIX :ap_l_div1:
%
% (second-rank candidate to rewrite in assembly)
%
% The quotient r[]/d is calculated, where d<>0.
% If quotient not needed, set q to pointer to r[1]
%
% Word ap_l_div1(q,r,l,d)
%
% Word *q // pointer to the LSW of the quotient
% Word *r // pointer to the LSW of the remainder/dividend
% Size l // size of the dividend, l>=1
% Word d // divisor
%
% Entry:
%
% q IS $0 % pointer to the LSW of the quotient
% r IS $1 % pointer to the LSW of the remainder/dividend
% l IS $2 % size of the dividend, l>=1
% d IS $3 % divisor
%
% Exit: quotient MSW; other words of quotient at array q
%
% Profile:
%
% 102 instructions
%
% d=3 r[0]=1 r[1]=2 ...
%
% l=1
% 11,2,15;1,2
%
% l=2
% 18,4,81;2,2
%
% l=5
% 191,10,348;5,2
%
% l=10
% 367,20,613;10,2
%
% l=20
% 717,40,1143;20,2
%
% l=50
% 1767,100,2733;50,2

```

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```

%
% l=100
% 3517,200,5383;100,2
%
% l=200
% 7017,400,10683;200,2
%
% l=500
% 17517,1000,26583;500,2
%
%
% PREFIX :ap_l_div2:
%
% (second-rank candidate to rewrite in assembly)
%
% The quotient r[]/(dl+dh*B) is calculated,
% where B=2^64 and dh<>0.
% If quotient not needed, set q to the address of r[2].
%
% Word ap_l_div2(q,r,l,dh,dl)
%
% Word *q // pointer to the LSW of the quotient
% Word *r // pointer to the LSW of the remainder/dividend
% Size l // size of the dividend, l>=1
% Word dh // MSW of the divisor
% Word dl // LSW of the divisor
%
% Entry:
%
% q IS $0 % pointer to the LSW of the quotient
% r IS $1 % pointer to the LSW of the remainder/dividend
% l IS $2 % size of the dividend, l>=2
% dh IS $3 % MSW of the divisor
% dl IS $4 % LSW of the divisor
%
% Exit: quotient MSW; other words of quotient at array q
%
% Profile:
%
% 279 instructions
%
% dh=3 dl=2 r[0]=1 r[1]=2 ...
%
% l=2
% 25,4,32;1,2
%
% l=5
% 165,10,482;9,3
%
% l=10
% 590,20,990;18,7
%
% l=20
% 1160,40,1920;38,7
%
% l=50
% 3035,100,4905;98,22
%
% l=100
% 6149,200,9867;198,46
%
% l=200
% 12388,400,19804;398,95

```

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```
l=500
31160,1000,49680;998,247
```

```
PREFIX :ap_l_div_class:
```

```
(third-rank candidate to rewrite in assembly)
```

```
The quotient d[]/s[] and the remainder are calculated
If quotient not needed, set q point to r[ls]
```

```
Word ap_l_div_class(q,r,l,dh,dl)
```

```
Word *q // pointer to the LSW of the quotient
Word *r // pointer to the LSW of the remainder/dividend
Size ld // size of the dividend
Word *s // pointer to the LSW of the source/divisor
Size ls // size of the divisor, ld>=ls>0
```

```
Entry:
```

```
q IS $0 % pointer to the LSW of the quotient
r IS $1 % pointer to the LSW of the remainder/dividend
ld IS $2 % size of the dividend
s IS $3 % pointer to the LSW of the source/divisor
ls IS $4 % size of the divisor, ld>=ls>0
```

```
Exit: quotient MSW; other words of quotient in array q
```

```
Profile:
```

```
583 instructions
```

```
r[0]=1001 r[1]=1002 ... s[0]=1 s[1]=2 ...
```

```
ls=5 ld=5
126,15,255;8,2
```

```
ls=5 ld=6
222,23,475;13,3
```

```
ls=5 ld=10
825,55,1401;29,14
```

```
ls=10 ld=10
196,30,384;13,2
```

```
ls=10 ld=11
362,53,705;23,3
```

```
ls=10 ld=20
2325,260,3835;103,31
```

```
ls=20 ld=20
336,60,600;23,2
```

```
ls=20 ld=21
642,113,1165;43,3
```

```
ls=20 ld=40
7345,1120,12057;405,57
```

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```
ls=50 ld=50
756,150,1290;53,2
```

```
ls=50 ld=51
1484,293,2545;103,3
```

```
ls=50 ld=100
41049,7864,66163;2700,133
```

```
ls=100 ld=100
1456,300,2440;103,2
```

```
ls=100 ld=101
2882,593,4845;203,3
```

```
ls=100 ld=200
154101,31346,249229;10603,265
```

```
ls=200 ld=200
2856,600,4740;203,2
```

```
ls=200 ld=201
5682,1193,9445;403,3
```

```
ls=200 ld=400
603769,127474,973865;42812,499
```

```
ls=500 ld=500
7056,1500,11640;503,2
```

```
ls=500 ld=501
14084,2993,23245;1003,3
```

```
ls=500 ld=1000
3832739,835969,6107675;279492,1169
```

```
KARASTUBA'S METHOD
```

```
PREFIX :kara:
```

```
kara(d,s1,s2,b1,b2,n) (fourth-rank candidate to rewrite in assembly)
```

```
The following routine do Karatsubas multiplication
recursively.
```

```
Entry: $0=d; $1=s1; $2=s2; $3=b1; $4=b2; $5=n
where d,s1,s2 are destination and source pointers,
respectively, b1 and b2 are buffer pointers.
b1=s1 and/or b2=s2 possible, in which case the
corresponding source(s) will be destroyed. Here n is
the length of the sources and the buffers.
The length of the destination is 2n.
Recursive halving and calls are used until the length
became smaller then the treshold constant.
```

```
Exit: -
```

```
Profile:
```


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```

Not yet written

PREFIX :kara_short:
kara_short(d,s1,s2,n)
(first-rank candidate to rewrite in assembly)

This routine works as kara, but
does everything in registers. On MMIX, it works for 1<=n<=7,
i.e. on MMIX the threshold is planned to be 8.
% Entry: $0=d; $1=s1; $2=s2; $3=n
% where d,s1,s2 are destination and source pointers,
% respectively, and n is
% the length of the sources and the buffers.
% The length of the destination is 2n.
% Exit: -
% Profile:
l= 1
  9,4,22;0,1
l= 2
 36,8,76;1,1
l= 3
 84,12,169;2,1
l= 4
151,16,299;3,1
l= 5
239,20,468;4,1
l= 6
346,24,672;6,0
l= 7
472,28,917;5,1

PREFIX :kara_sqr:
kara_sqr(d,s,b,n)
(fourth-rank candidate to rewrite in assembly)

The following routine do Karatsubas squaring
recursively.
% Entry: $0=d; $1=s; $2=b; $3=n
% where d,s are destination and source pointers,
% respectively, b is a buffer pointer.
% b=s possible, in which case the
% source will be destroyed. Here n is
% the length of the source and the buffer.
% The length of the destination is 2n.
% Recursive halving and calls are used until the length
% became smaller then the treshold constant.

```

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```

% Exit: -
% Profile:
% Not yet written
% PREFIX :kara_sqr_short:
% (first-rank candidate to rewrite in assembly)
% This routine works as kara_sqr, but
% does everything in registers. On MMIX, it works for 1<=n<=7,
% i.e. on MMIX the treshold is planned to be 8.
% Entry:
d IS $0 % pointer to the LSW of the destination
s IS $1 % pointer to the LSW of the source
l IS $2 % length of sources in words, always positive
% Exit: -
% Profile:
l= 1
  7,2,20;0,1
l= 2
 33,5,64;1,1
l= 3
 66,8,124;2,1
l= 4
109,11,203;3,1
l= 5
162,14,301;4,1
l= 6
225,17,416;6,0
l= 7
296,20,552;5,1

% FOURIER TRANSFORMATION OVER THE COMPLEX NUMBERS

% SPARSE NUMBERS

% FOURIER TRANSFORMATION MODULO A FERMAT NUMBER

```

% FAST NATURAL NUMBER ARITHMETIC

% MODULAR ARITHMETIC